



Temperature dependences of N₂-broadening and shift coefficients in the ν₆ perpendicular band of ¹²CH₃D



A. Predoi-Cross ^{a,*}, V. Malathy Devi ^b, K. Sung ^c, T. Sinyakova ^d, J. Buldyreva ^d,
D. Chris Benner ^b, M.A.H. Smith ^e, A.W. Mantz ^f

^a Department of Physics and Astronomy, University of Lethbridge, Lethbridge, AB, Canada T1K 6R4

^b Department of Physics, The College of William and Mary, Williamsburg, VA 23187, USA

^c Jet Propulsion Laboratory, California Institute of Technology, Pasadena, CA 91109, USA

^d Institute UTINAM UMR CNRS 6213, University of Franche-Comte, 25030 Besancon, France

^e Science Directorate, NASA Langley Research Center, Hampton, VA 23681, USA

^f Department of Physics, Astronomy and Geophysics, Connecticut College, New London, CT 06320, USA

ARTICLE INFO

Article history:

Received 19 March 2015

Received in revised form

11 May 2015

Accepted 12 May 2015

Available online 22 May 2015

Keywords:

Monodeuterated methane

Infrared spectra

Nitrogen-broadening

Temperature dependences of widths and shifts

Line mixing

Spectral line shapes

ABSTRACT

The temperature-dependences of line broadening and shift parameters for many ¹²CH₃D transitions have been determined using six high-resolution, high signal-to-noise ratio, room-temperature CH₃D (98% purity) and CH₃D-N₂ spectra recorded with 25 cm path length (at 0.01 cm⁻¹ unapodized resolution) using the McMath–Pierce FTS located on Kitt Peak, Arizona, and 17 additional high quality, pure CH₃D (99% purity) and CH₃D-N₂ spectra recorded between 79 and 296 K with the 20.38 cm path coolable cell (at 0.0056 cm⁻¹ unapodized resolution) with the Bruker 125HR FTS at the Jet Propulsion Laboratory (JPL), Pasadena, California. The spectra have been fitted simultaneously applying a multispectrum nonlinear least-squares technique. In the analysis, the Lorentzian N₂-broadened half-width coefficients and the corresponding pressure-shift coefficients as well as their temperature dependences are extracted for about 400 transitions ($0 \leq J'' \leq 19$, $K'' \leq 16$) in the perpendicular ($\Delta K = \pm 1$) ν₆ band. At 296 K, the measured N₂-broadened half-width coefficients range from 0.0209 to 0.0782 cm⁻¹ atm⁻¹ whereas the majority of the associated N₂-induced shift coefficients are negative, and the values are between -0.016 and 0.005 cm⁻¹ atm⁻¹. The temperature dependence exponents for N₂-broadened half-widths range between 0.264 and 0.924, whereas the temperature dependence coefficients for N₂-induced shifts are between 0 and 0.00011 cm⁻¹ atm⁻¹ K⁻¹. The N₂-broadened half-width coefficients have been also calculated using a semi-classical approach based on a rigorous treatment of the active molecule as a symmetric top, a model intermolecular potential comprising both short- and long-range interactions, and exact classical trajectories. The role of the various high-order multipoles in the line-broadening at low, middle and high values of the rotational quantum number J'' has been investigated and the main features of the K-dependences analyzed. The calculations performed for 296, 240 and 190 K have allowed to deduce the half-width temperature-dependence exponents, completing the general comparison of our new experimental results with those which are available in the literature.

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* Corresponding author. Tel.: +1 403 329 2697; fax: +1 403 329 2057.

E-mail address: adriana.predoi-cross@uleth.ca (A. Predoi-Cross).

1. Introduction

Methane is a prominent atmospheric trace gas and the third most abundant greenhouse gas in many regions of the world [1,2]. The sources of methane are both natural, such as wetlands and methane-outgassing from oceans [3], and anthropogenic, such as animal husbandry and fossil-fuel extraction [4]. The methane sinks include processes in atmospheric chemistry such as reactions with hydroxyl radicals [5] and natural processes in soil [6].

Besides the main isotopologue CH₄, the monodeuterated species CH₃D is highly important for understanding various atmospheric processes. In the Earth's atmosphere, stratospheric profiles of CH₃D mixing ratios have been retrieved using high-resolution solar occultation infrared spectra from the Atmospheric Trace MOlecle Spectroscopy (ATMOS) satellite instrument [7,8] and references therein. CH₃D is also an isotopic tracer present (or expected to be present) in many planetary atmospheres such as those of Jupiter, Saturn [9–11], Uranus [12–14], Mars [15–18], Titan [19–23], and subject to transport and chemical effects. It has also been identified in cometary spectra [24,25]. The concentrations of CH₃D and those of the parent molecule CH₄ are used to calculate the D/H ratios in these celestial bodies [26].

The atmosphere of Titan contains about 5% of methane and mostly nitrogen. The Composite InfraRed Spectrometer (CIRS) instrument on the Cassini spacecraft is monitoring Titan's thermal emission spectrum through three focal planes, one of them covering the spectral range of the CH₃D ν_6 band [23]. Knowledge of the temperature-dependence of N₂-broadened line widths and shifts over the Titan atmospheric temperature range (70–200 K) is needed for correct interpretation of IR spectra of Titan's atmosphere, such as those obtained by the CIRS instrument (for example, [23]). Bands of the three most abundant methane isotopologues (¹²CH₄, ¹³CH₄ and CH₃D) in the spectral region from 6 to 10 microns are used not only for detection of atmospheric composition, but also for retrievals of Titan atmospheric temperature profiles and determination of ¹³C/¹²C and D/H ratios [23,26].

Most of the measured methane line widths happen to increase as a power law when temperature is decreasing. There have been several spectroscopic studies related to the spectral line shapes (e.g., Lorentz widths, pressure-shifts) of the ν_6 band of CH₃D [27–35]. N₂-broadened widths and N₂-induced shifts of ¹²CH₃D lines have been measured at room temperature for transitions in the ν_2 [36], ν_3 [37–39], ν_5 [40], ν_6 [35], and $2\nu_4$ [41] bands. For low temperatures, measurements of only 10 N₂-broadened line-width coefficients of individual CH₃D lines in the ν_2 [42], ν_3 and ν_6 [43] bands are available in the literature, and spectroscopic databases (e.g., HITRAN [44]) currently list only a constant default value for the temperature dependences of the CH₃D line widths. Reports of selected room-temperature line mixing via off-diagonal relaxation matrix element coefficients for transitions of CH₃D broadened by N₂ in the ν_3 [39], ν_5 [40], and ν_6 [35] bands.

In 2002 [35] we reported Lorentz self- and nitrogen-broadened line-width coefficients as well as corresponding line-shift coefficients for more than 480 transitions in

six sub-branches (^PP, ^PQ, ^PR, ^RP, ^RQ, ^RR) of the ν_6 (E) perpendicular band of ¹²CH₃D. These results were obtained from multispectrum fits of 14–17 spectra recorded at room temperature in the 1035–1270 cm^{−1} spectral range using two different Fourier-transform spectrometers, namely the McMath–Pierce FTS formerly located on Kitt Peak, Arizona, and the Bruker IFS 120 HR FTS located at the Pacific Northwest National Laboratory, Richland, Washington. The spectra were recorded using absorption path lengths of 10, 19.95, 25, 150, and 2486 cm, respectively. The gas total pressures ranged from 0.11 to 303 Torr for pure CH₃D and from 103 to 403 Torr for lean mixtures (~0.01 volume mixing ratios) of CH₃D and nitrogen.

To retrieve the temperature dependences of line-shape parameters, 17 new spectra of both pure (99%) CH₃D and dilute mixtures (0.003–0.0164 volume mixing ratios) of the same high-purity CH₃D sample in research grade nitrogen have been recorded from room to low temperatures using the coolable absorption cell with a path length of 20.38 cm (see [45] for its detailed description). The simultaneous multispectrum analysis [46] of the 17 new spectra and the six previous spectra [35] has allowed the determination of N₂-broadened line-width and N₂-pressure-induced line-shift coefficients and their temperature dependences for a large number of transitions. In addition, N₂-line mixing coefficients for 17 pairs of transitions via the off-diagonal relaxation matrix element formalism [46,47] have been also obtained.

However, unlike the line-width and pressure-shift coefficients, the temperature dependences of the relaxation matrix element coefficients could not be determined reliably for all measured mixed pairs. In such instances, a default value of 0.75 has been applied for other line-mixed pairs in the least squares fittings.

2. Experimental details and data analysis

As mentioned above, six of the 23 infrared absorption spectra analyzed in this study were from the set of room-temperature spectra previously used to study N₂- and self-broadening in ¹²CH₃D transitions in the Triad region [35,36,40]. These spectra were recorded using the Kitt Peak FTS with an unapodized resolution of 0.01 cm^{−1} and signal-to-noise (S/N) ratios of about 700 and covered the spectral region 690–2840 cm^{−1}. Two of the six spectra recorded at low-pressure (1–3 Torr) and high-purity (98% enriched CH₃D from ICON isotopes) were important in the present study to determine the “zero-pressure” line centers of the ¹²CH₃D transitions.

A set of 17 new high-resolution (0.0056 cm^{−1}), high S/N (> 1000) spectra were recorded in 2010 covering the 1070–1540 cm^{−1} spectral region, using the Bruker IFS 125HR Fourier transform spectrometer at the Jet Propulsion Laboratory. For recording these new spectra a specially designed and built 20.38 cm straight-path coolable absorption cell [45] was used. Various CH₃D and CH₃D+N₂ gas pressures, temperatures and volume mixing ratios of CH₃D were used to obtain these experimental spectra. A few low-pressure pure CH₃D spectra were acquired with the Bruker FTS as well, in order to more accurately

Table 1

Details on the experimental setup and physical conditions of spectra.

Configuration and conditions	JPL FTS Bruker 125 HR	McMath-Pierce Kitt Peak FTS
Useable band pass (cm^{-1})	1000–1540	1050–2400
Light source	Globar	Globar
Beam splitter	KBr	KCl
Detector	HgCdTe	He cooled As:Si
Resolution (cm^{-1}) (unapodized)	0.0056	0.01
Maximum optical path difference (cm)	90.00	49.99
Aperture diameter (mm)	1.5	8
Sample pressure (Torr)	See Table 2	See Table 2
Temperature ^c (K)	79–296 K	296.0–296.6 K
Cell path length (cm)	20.38	25 cm
Cell windows (wedge)	KBr	KCl
Scanning time (hours)	~2	1.1 (10 coadds)
Signal-to-noise	~1100–1800	~700
Calibration standards	ν_2 lines H ₂ O [48]	ν_2 lines H ₂ O [48]

Table 2Summary of the experimental conditions of the CH₃D spectra.

Temperature (K)	Gas mixture	CH ₃ D VMR	Path (cm)	Pressure (Torr)	Calibration correction ^a	RMS ^b
296.60	CH ₃ D	1.0	25.0	1.013	0.999998059	0.115
295.45	CH ₃ D	1.0	25.0	3.050	0.999998708	0.113
296.20	CH ₃ D+N ₂	0.0133	25.0	102.50	0.999997940	0.105
296.40	CH ₃ D+N ₂	0.0133	25.0	202.10	0.999998054	0.099
296.40	CH ₃ D+N ₂	0.0133	25.0	302.55	0.999998144	0.104
296.40	CH ₃ D+N ₂	0.0136	25.0	402.25	0.999998200	0.112
296.00	CH ₃ D+N ₂	0.00362	20.38	250.60	1.0000002644	0.088
296.00	CH ₃ D+N ₂	0.00365	20.38	728.94	1.0000002853	0.093
239.65	CH ₃ D+N ₂	0.00983	20.38	194.99	1.0000002702	0.091
240.15	CH ₃ D+N ₂	0.01575	20.38	444.04	1.0000002712	0.110
239.65	CH ₃ D+N ₂	0.00990	20.38	602.23	1.0000002710	0.098
189.65	CH ₃ D	1.0	20.38	7.10	1.0000002625	0.100
188.65	CH ₃ D+N ₂	0.01302	20.38	152.72	1.0000002738	0.088
188.65	CH ₃ D+N ₂	0.0037	20.38	256.82	1.0000002616	0.079
189.15	CH ₃ D+N ₂	0.0133	20.38	546.30	1.0000002669	0.096
135.15	CH ₃ D	1.0	20.38	2.58	1.0000002747	
133.35	CH ₃ D+N ₂	0.00512	20.38	177.67	1.0000002771	0.085
133.35	CH ₃ D+N ₂	0.01635	20.38	246.38	1.0000002758	
133.35	CH ₃ D+N ₂	0.00515	20.38	503.86	1.0000002739	0.085
78.75	CH ₃ D	1.0	20.38	8.5	1.0000002744	
77.65	CH ₃ D+N ₂	0.0127	20.38	100.90	1.0000002796	0.094
75.15	CH ₃ D+N ₂	0.00339	20.38	295.28	1.0000002774	0.092
76.95	CH ₃ D+N ₂	0.0119	20.38	642.12	1.0000002788	

Note: 760 Torr = 1 atm = 101.325 kPa.

^a Wavenumber scales were calibrated relative to ν_2 water vapor line positions by Toth [48].^b The RMS values correspond to the multispectrum fit residuals plotted in Fig. 3(b).

determine the zero-pressure line positions (since these spectra had higher resolution than the low-pressure Kitt Peak spectra).

All 23 spectra were simultaneously fitted using a multispectrum nonlinear least-squares technique [46]. Details on the experimental setups for the two sets of measurements are provided in Table 1. The experimental physical conditions of the spectra analyzed are presented in Table 2. Transitions belonging to all bands in the Triad (ν_3 , ν_6 and ν_5) were observed in both sets of spectra. Spectroscopic results pertaining to only the ν_6 perpendicular band of ¹²CH₃D will be presented in this article. Results for the parallel band ν_3 and the perpendicular band ν_5 will be reported in a subsequent article.

3. Retrievals of line parameters

Prior to the multispectrum fittings the wavenumber scales of both datasets were calibrated using reference water vapor line positions [48]. In the case of Kitt Peak data, these water vapor lines had two components, a narrow line due to residual gas in the evacuated FTS chamber as well as a broad feature from atmospheric-pressure optical paths outside the FTS and sample cell purged with dry nitrogen vapor to minimize H₂O absorptions interfering with the CH₃D transitions. In the JPL Bruker spectra, the water lines arose only from small amounts of residual gas in the evacuated FTS chamber. The wavenumber calibration factors determined for each

of the fitted spectra are included in **Table 2**. In both sets of experiments, the sample pressures and temperatures were continually monitored during the measurements using appropriate calibrated pressure gauges and temperature sensors [35,45].

The spectral line parameters in the HITRAN2008 database [49] were used as initial guesses for starting the multispectrum fittings. Before starting the fits, it was also necessary to establish the isotopologue abundances (e.g., $^{12}\text{CH}_4$, $^{13}\text{CH}_4$, $^{12}\text{CH}_3\text{D}$ and $^{13}\text{CH}_3\text{D}$) in the CH_3D samples. Initial estimates of the isotopologue abundances were made based upon the % D-enrichments stated by the manufacturer (ICON Isotopes). Small adjustments to these isotopologue abundances were needed when the spectra were fit simultaneously. These values were established by fitting several selected regions of each spectrum prior to analyzing all of the fitted regions. Once the isotopologue abundances were determined, they remained the same for the corresponding spectra in all fitted regions.

Low-pressure pure CH_3D spectra at room temperature were fitted first and N_2 -broadened spectra at room temperature were then added, one spectrum at a time, until all room-temperature spectra were fitted simultaneously. This process allowed the initial determination of room temperature N_2 -broadened width and shift coefficients for the strong, unblended lines. Subsequently, low temperature pure CH_3D and N_2 -broadened CH_3D spectra were added one spectrum at a time, as appropriate. The volume mixing ratios of N_2 -broadened spectra were carefully adjusted (when appropriate) while the temperature dependences of Lorentz self- and N_2 -broadened width and shift coefficients of various lines were adjusted until all the spectra were fit satisfactorily such that the weighted (observed minus calculated) fit residuals from all fitted spectra were minimized and no noticeable features were observed in the residuals.

N_2 - and self-broadened line-width, pressure-shift and the relaxation matrix element coefficients (where appropriate) were retrieved using the multispectrum fitting procedure that has been described in several of our prior studies (for example: [34–36,39–40,46–47]). Spectral intervals of 5–15 cm^{-1} wide from each of the 23 spectra were fitted simultaneously. The total number of spectra fitted in each interval varied between 19 and 23, depending upon whether $^{12}\text{CH}_3\text{D}$ features were apparent at the volume mixing ratios and gas sample pressures of the chosen spectra. For strong CH_3D transitions the line positions, intensities, N_2 -broadening coefficients and their temperature dependence exponents, N_2 -induced shift coefficients and their temperature dependence coefficients were adjusted until the sum of the squares of the weighted fit residuals between the observed and calculated line profiles were minimized.

Line mixing (off-diagonal relaxation matrix element, or ORME) coefficients between selected pairs of transitions were also determined, where possible. Even though the temperatures of the gas samples ranged between 296 K and 75 K, in several cases, it was not possible to measure with confidence the temperature dependences of the relaxation element coefficients. An improved theoretical model for the temperature-dependence of CH_3D line

mixing is needed to measure these parameters correctly and reliably. Where their values were not determined, the temperature dependence exponents were fixed to a default value of 0.75, similar to the default value applied for the temperature dependence exponents of the line-width coefficients..

Although several (see **Table 2**) pure CH_3D spectra were included in the analysis, the pressures were not high enough to retrieve reliable information on self-broadening and self-shift coefficients for all observed transitions. The pure CH_3D gas pressures were in an intermediate range so that we could not completely ignore their values. This means that in some instances (e.g., low-temperature spectra) it was necessary to adjust the self-broadening and its temperature dependence exponent to obtain a best fit. However, while many self-broadening coefficients and their temperature dependences could be determined from our spectra, it was not possible to measure any reliable self-pressure-shift coefficients or their temperature dependence coefficients.

As in previous studies using the multispectrum fitting technique, the Lorentz N_2 -broadened line-width coefficients, N_2 -induced line-shift coefficients and their temperature dependences were measured on a line-by-line basis using the following equations:

$$b_L(p, T) = p \left[b_L^0(N_2)(p_0, T_0)(1-\chi) \left[\frac{T_0}{T} \right]^{n_1} + b_L^0(\text{self})(p_0, T_0)\chi \left[\frac{T_0}{T} \right]^{n_2} \right] \quad (1)$$

$$\nu = \nu_0 + p [\delta^0(N_2)(1-\chi) + \delta^0(\text{self})\chi] \quad (2)$$

$$\delta^0(T) = \delta^0(T_0) + \delta'(T - T_0) \quad (3)$$

where b_L^0 and δ^0 represent pressure broadening and pressure-shift coefficients (in $\text{cm}^{-1} \text{atm}^{-1}$ at $T_0=296 \text{ K}$), respectively. $b_L(p, T)$ is the Lorentz half-width (in cm^{-1}) of the spectral line at pressure p and temperature T , $b_L^0(\text{Gas})$ (p_0, T_0) is the Lorentz half-width coefficient of the line at the reference pressure p_0 (1 atm) and temperature T_0 of the broadening gas (either N_2 or CH_3D). χ is the ratio of the partial pressure of CH_3D to the total gas pressure in the cell. The temperature dependence coefficients of the Lorentz half-width coefficient are n_1 (for N_2) and n_2 (for CH_3D). The temperature dependence of the N_2 -pressure-shift coefficients is $\delta'(N_2)$. Temperature dependences of N_2 - and self-broadened (in a few cases) half-width and pressure-induced shift coefficients were measured separately for each transition within the same fit. As shown in Eq. (3) a linear law was used for to model the temperature dependences of pressure-induced shift coefficients.

Self- and N_2 -broadened widths and the temperature dependence exponents for the broadening coefficients for all transitions were initially fixed to values in the HITRAN2008 database [49] and depend upon the rotational quantum numbers of the transition. Indeed, in the HITRAN databases ([44,49]) only the self- and air-broadened line-width coefficients are listed and we have assumed that the N_2 -width coefficients for the unmeasured transitions are the same as the air-broadened width coefficients. For parameters not

included in HITRAN [44,49], the initial values for all transitions were set at reasonable default values estimated from our previous studies of CH₃D [35], ¹²CH₄ and ¹³CH₄ [50–53] in the thermal infrared. The pressure-broadened self- and N₂-width, self- and N₂-shift coefficients and their temperature dependence values were 0.085 cm⁻¹ atm⁻¹, 0.065 cm⁻¹ atm⁻¹, -0.003 cm⁻¹ atm⁻¹, -0.002 cm⁻¹ atm⁻¹, 0.75 and 0.75, respectively. The temperature-dependence coefficients for self- and N₂-induced shift for all lines were initially set to default values of 0.00002 cm⁻¹ atm⁻¹ K⁻¹ instead of zero, based upon our previous studies of self- and air-broadening in ¹²CH₄ and ¹³CH₄ [50–53] in the same spectral region. For unmeasured lines the parameters remained fixed to these default values. This assumption introduced no noticeable residuals in the least squares fits (see Figs. 3 and 4).

For weaker transitions for which broadening and shift coefficients could not be determined, only their line positions and intensities were adjusted in the multispectrum fits. Several weak unidentified features (trace contaminants of unknown origin or ¹³CH₃D transitions) appeared in some of the fitted regions and were included as unidentified transitions in the fit. The broadening and shift parameters of these unidentified features remained fixed to the default values described above.

During the analysis, it was noticed that, in order to minimize the fit residuals, the gas sample temperatures, especially for the lowest temperature (~ 79 K) dataset, apparently needed adjustments in the range -0.5 to -4.2 K from the ones given by the temperature sensors during the experiments. These adjustments were required in order to fit all of the spectra using the power-law expression (Eq. (1)) for temperature dependence of the line-widths, and the adjusted

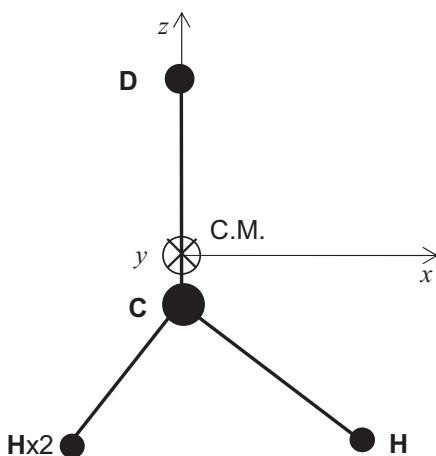


Fig. 1. Molecular frame and geometry parameters for the CH₃D molecule: |CH| = |CD| = 1.08601 Å [60], $\angle DCH = 109.46667^\circ$.

temperatures may not necessarily represent the actual physical temperatures of the gas samples. Departures from the power law have been evidenced by others and this confirms that such a law is approximate and that efforts in the theory are needed to derive more elaborate dependences.

At this time, we would like to attribute this need for temperature adjustments to be related to the small departures from the power-law temperature dependence of the Lorentz line-width coefficients that were observed over the same temperature range with the fit of the ¹³CH₄ R(2) manifold (See Ref. [45] and references cited therein). With this temperature adjustment we were still able to use Eq. (1) to obtain best-fit residuals in all our fitted intervals (e.g., Figs. 3 and 4). In the present analysis we have not made further efforts to fully characterize this temperature behavior of the Lorentz width coefficients, and our measured line-width coefficients could be characterized as the “effective line-width coefficients” with their temperature dependence exponents still enforced by Eq. (1). The actual temperature values used in the fits are listed in Table 2 rather than the measured temperatures so that the resulting effective line-width parameters can be compared with future experimental studies.

4. Theoretical modeling of N₂-broadening coefficients and their temperature dependences for CH₃D transitions

Theoretical estimations of pressure-broadened CH₃D line widths were performed solely for the case of perturbation by nitrogen. Indeed, for this active molecule with a very small electric dipole moment (0.057 D [54]) and a vanishing quadrupole moment, the long-range interactions with an identical partner are very weak whereas the short-range interactions (typically modeled by pairwise atom-atom Lennard-Jones potentials) are determined by atom-atom parameters whose values are available in the literature. We note that the parameter values from different sources are sometimes inconsistent. For collisions with nitrogen, the intermolecular potential is expected to be modeled in a more reliable manner because of stronger electrostatic interactions.

Table 4

Atomic distances to the molecular centers of mass (calculated with the geometry of Fig. 1 for CH₃D and taken from [61] (for N₂) and atom-atom Lennard-Jones parameters [65] (for CH₃D-N₂ interactions).

r_{1i}, r_{2j} (Å)	$d_{ij} (10^{-7} \text{ erg } \text{\AA}^{12})$	$e_{ij} (10^{-10} \text{ erg } \text{\AA}^6)$
$r_{1C}=0.0641$	$d_{CN}=0.3234$	$e_{CN}=0.2922$
$r_{1D}=1.0219$	$d_{HN}=0.0571$	$e_{HN}=0.0803$
$r_{1H}=1.1090$	$d_{DN}=0.0571$	$e_{DN}=0.0803$
$r_{2N}=0.550$		

Table 3

Molecular parameters for CH₃D and N₂ used in the calculations: dipole moments μ , quadrupole moments Q , octopole moments Ω , mean polarizabilities α , polarizability anisotropies γ and hyper-polarizabilities $A_{||}$ and A_{\perp} ($\alpha, \gamma, A_{||}$ and A_{\perp} for CH₃D are those of CH₄).

Molecule	μ (D)	Q (D Å)	Ω (D Å ²)	α (Å ³)	γ	$A_{ }=A_{\perp}$ (Å ⁴)
CH ₃ D	0.057 [54]	0	3.10 [62]	2.59 [63]	0	0.82 [37]
N ₂	0	-1.3 [61]	0	1.74 [63]	0.137 [64]	0

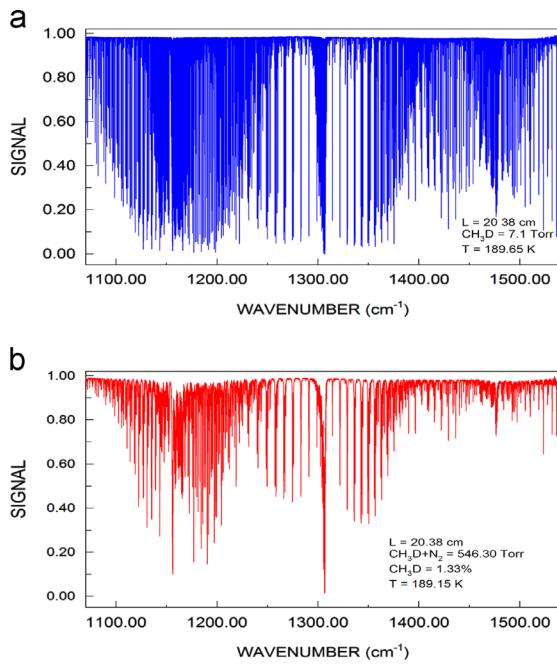


Fig. 2. Two laboratory absorption spectra of $^{12}\text{CH}_3\text{D}$ in the Triad region between 1070 and 1540 cm^{-1} recorded at 0.0056 cm^{-1} resolution with the Bruker FTS at JPL. The spectrum shown in the top panel (a) corresponds to 99% pure $^{12}\text{CH}_3\text{D}$ sample and the one shown in the bottom panel (b) is a dilute mixture of the 99% high-purity $^{12}\text{CH}_3\text{D}$ sample in nitrogen. Both spectra were taken near 189 K and using the 20.38 cm coolable cell (see text for details).

Calculations of N_2 -broadened line widths in the ν_6 band of CH_3D were performed with the standard expression of the semi-classical formalism of Robert and Bonamy [55]:

$$\gamma_{if} = \frac{n_2 \bar{V}}{2\pi c} \int_0^\infty 2\pi b db \langle 1 - e^{-\text{Re } S_2} \rangle_{J_2} \quad (4)$$

where γ_{if} (in cm^{-1}) is the half-width of the line corresponding to the radiative transition $i \rightarrow f$. n_2 is the number density of the perturbing molecules; $\bar{V} = \sqrt{8kT/\pi m^*}$ is the mean relative thermal velocity (k is the Boltzmann constant, T is the temperature in Kelvin and m^* is the reduced mass of the molecular pair). The real part of the second-order contribution to the scattering matrix S_2 is averaged over the J_2 rotational states of the perturbing gas and integrated over the impact parameter b . We notice that the modified formula suggested by Ma et al. [56] and performing the average over J_2 states as the cumulated average (inside the exponential function) leads to overestimated values, so that we preferred not to employ it for our calculations.

The integration over trajectories required for computations of various S_2 terms was made with the exact-trajectory model [57–59] and the rotationally invariant representation of the interaction potential between the active (indexed by 1) and the perturbing (indexed by 2) molecules:

$$V(1, 2, \vec{r}) = \sum_{l_1 l_2 l_1 k_1} V_{l_1 l_2 l_1}^{k_1}(r) \sum_{m_1 m_2 m} C_{l_1 m_1 l_2 m_2}^{lm} D_{m_1 k_1}^{l_1} * \\ \times (\varphi_1, \theta_1, \chi_1) D_{m_2 0}^{l_2} * (\varphi_2, \theta_2, \chi_2) C_{lm}(\theta, \varphi) \quad (5)$$

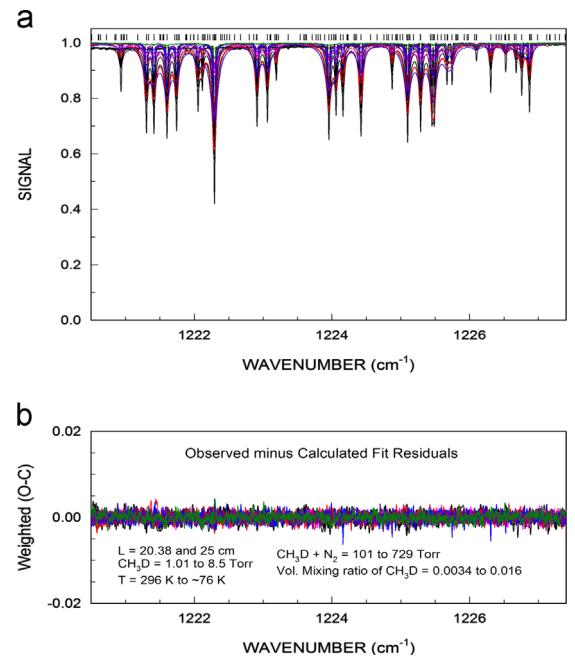


Fig. 3. A sample fitted interval in the $^{12}\text{CH}_3\text{D}$ Triad. Transitions belonging to both the ν_3 and ν_6 bands appear in this region. The experimental spectra are plotted in the upper panel (a) and the weighted observed minus calculated differences are shown in the lower panel (b). 20 of the possible 23 spectra are included in the fit. Small residuals (< 1% deep) still persist in one of the spectra that could not completely be fitted out. Some of these could belong to $^{13}\text{CH}_3\text{D}$ transitions for which assignments were not available when the present analysis was performed. Color codes: room-temperature spectra with the 25 cm cell (black); room-temperature spectra with the 20.38 cm cell (pink); spectra at 240 K (red); spectra at 189 K (blue); spectra at ~ 135 K (dark pink); spectra at ~ 76 K (dark green). (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

In this equation the products of rotational Wigner matrices and the spherical harmonics C^{lm} (normalized to $\sqrt{4\pi/(2l+1)}$) $D_{m_1 k_1}^{l_1}(\varphi_1, \theta_1, \chi_1) D_{m_2 0}^{l_2}(\varphi_2, \theta_2, \chi_2) C_{lm}(\theta, \varphi)$ represent the rotationally invariant basis in the laboratory fixed frame (asterisks mark the complex conjugation), $C_{l_1 m_1 l_2 m_2}^{lm}$ are the Clebsch–Gordan coefficients. The radial potential components $V_{l_1 l_2 l}^{k_1}(r)$ contain contributions from various kinds of intermolecular interactions. We expressed the potential as a sum of electrostatic (e), induction (i) and dispersion (d) long-range terms completed by pairwise atom–atom (a) terms accounting for the short-range forces (the explicit forms of radial potential components and second-order contributions to the scattering matrix can be found in [59]).

Contrary to a previous simplified semi-classical calculation for the ν_2 parallel band [36] in which the three hydrogen atoms were projected on the principal molecular symmetry axis to form a linear molecule with CH_3D , we kept the real geometry of the equilibrium configuration (see Fig. 1), i.e. accurately treating the active molecule as a symmetric top. Because of the important role of the atom–atom terms in the quite weakly interacting $\text{CH}_3\text{D}-\text{N}_2$ system this more realistic configuration of hydrogen atoms is expected to ensure a better description of intermolecular interactions and more reliable line width values. After

Table 5

Experimental and calculated N₂-broadened line parameters and experimental self-broadened line parameters [see Eqs. (1–3) for the notations] in the ν₆ band of CH₃D. S are the symmetry labels and the ' and '' refer to the upper and lower states corresponding to each transition.

Position, cm ⁻¹	J	K'	S'	J''	K''	S''	Assignment	Int*10 ^{25a}	$b_L^0(N_2)$ expt. ^b	$b_L^0(N_2)$ calc. ^b	n_1 expt	n_1 calc.	$\delta^0(N_2)$ expt. ^b	$\delta'(N_2)$ expt ^c	$b_L^0(\text{self})$ expt ^b	n_2 expt
1080.746222(15)	10	3	E	11	4	E	^P P(11,4,E)	8.75(2)	0.0569(3)	0.0562	0.750(24)	0.630(1)				
1080.941134(7)	8	1	A1	9	0	A2	^R P(9,0,A2)	18.98(2)	0.0635(2)	0.0608	0.811(7)	0.678(4)	-0.00251(16)	0.0836(9)	0.798(14)	
1082.344848(29)	7	4	A2	8	3	A1	^R P(8,3,A1)	5.34(1)	0.0620(2)	0.0597	0.802(5)	0.665(4)	-0.00306(9)	0.0879(9)	0.0879(9)	
1082.349885(23)	7	4	A1	8	3	A2	^R P(8,3,A2)	5.22(1)	0.0620(2)	0.0597	0.802(5)	0.665(4)	-0.00306(9)	0.0879(9)	0.0879(9)	
1082.847607(20)	12	8	A1	13	9	A2	^P P(13,9,A2)	10.18(2)	0.0487(3)	0.0558	0.762(30)	0.618(1)	-0.00250(22)			
1083.497562(20)	11	6	E	12	7	E	^P P(12,7,E)	7.87(2)	0.0523(3)	0.0547	0.626(32)	0.614(1)	-0.00310(31)			
1084.418423(13)	10	4	E	11	5	E	^P P(11,5,E)	10.21(2)	0.0537(3)	0.0552	0.807(21)	0.620(1)	-0.00309(25)			
1085.228424(9)	7	3	E	8	2	E	^R P(8,2,E)	9.04(1)	0.0591(3)	0.0602	0.882(11)	0.670(4)		0.0881(6)		
1085.625324(8)	9	2	A2	10	3	A1	^P P(10,3,A1)	10.91(1)	0.0633(2)	0.0581	0.832(15)	0.649(2)	0.000027(2)	0.0893(8)		
1085.738824(8)	9	2	A1	10	3	A2	^P P(10,3,A2)	10.91(1)	0.0633(2)	0.0581	0.832(15)	0.649(2)	0.000027(2)	0.0893(8)		
1086.841190(42)	13	11	A2	14	12	A1	^P P(14,12,A1)	5.71(2)	0.0459(4)	0.0571		0.619(1)		0.0652(58)		
1087.149109(38)	12	9	E	13	10	E	^P P(13,10,E)	5.03(2)	0.0454(4)	0.0572		0.625(1)		0.0562(48)		
1087.570898(36)	11	7	E	12	8	E	^P P(12,8,E)	8.29(5)	0.0585(4)	0.0562	0.816(39)	0.624(1)	-0.00374(34)	0.000058(6)		
1087.887154(20)	6	5	E	7	4	E	^R P(7,4,E)	2.26(1)	0.0685(8)	0.0636		0.718(7)		0.0938(15)		
1088.082184(6)	7	2	E	8	1	E	^R P(8,1,E)	15.04(2)	0.0633(2)	0.0613	0.812(6)	0.682(5)	-0.00216(19)	0.0861(4)		
1088.252595(9)	10	5	A1	11	6	A2	^P P(11,6,A2)	22.65(3)	0.0527(1)	0.0553	0.712(10)	0.620(1)	-0.00307(11)			
1089.248131(10)	9	3	E	10	4	E	^P P(10,4,E)	13.36(2)	0.0565(2)	0.0569	0.755(13)	0.636(1)	-0.00351(19)			
1089.902710(5)	7	1	A2	8	0	A1	^R P(8,0,A1)	23.99(2)	0.0647(1)	0.0620	0.827(4)	0.690(5)	-0.00261(12)	0.0871(3)		
1090.645206(9)	8	1	E	9	2	E	^P P(9,2,E)	11.93(2)	0.0632(3)	0.0602	0.726(12)	0.671(3)	-0.00279(24)	0.000038(4)	0.0867(7)	
1090.725700(7)	6	4	A1	7	3	A2	^R P(7,3,A2)	9.87(1)	0.0656(3)	0.0618	0.792(7)	0.689(6)		0.094(5)		
1091.611499(38)	12	10	E	13	11	E	^P P(13,11,E)	5.21(2)	0.0462(4)	0.0580		0.630(1)				
1091.797634(12)	11	8	A2	12	9	A1	^P P(12,9,A1)	17.08(2)	0.0510(2)	0.0577	0.675(16)	0.635(1)	-0.00280(14)			
1092.239570(12)	10	6	E	11	7	E	^P P(11,7,E)	12.47(2)	0.0520(2)	0.0565	0.727(18)	0.631(1)				
1092.986295(9)	9	4	E	10	5	E	^P P(10,5,E)	15.69(2)	0.0557(2)	0.0562	0.751(12)	0.628(1)	-0.00245(16)	0.000036(3)		
1093.662989(7)	6	3	E	7	2	E	^R P(7,2,E)	8.98(1)	0.0620(2)	0.0616	0.813(7)	0.682(5)		0.0878(5)		
1094.044024(5)	8	2	A1	9	3	A2	^P P(9,3,A2)	16.06(1)	0.0642(2)	0.0590	0.774(6)	0.658(3)	-0.00214(11)	0.000023(1)	0.0893(4)	
1094.117524(5)	8	2	A2	9	3	A1	^P P(9,3,A1)	16.06(1)	0.0642(2)	0.0590	0.774(6)	0.658(3)	-0.00214(11)	0.000023(1)	0.0893(4)	
1095.705469(8)	7	0	E	8	1	E	^P P(8,1,E)	9.59(2)	0.0652(3)	0.0620	0.792(9)	0.689(5)	-0.00381(25)	0.0858(14)	0.788(18)	
1096.184869(20)	11	9	E	12	10	E	^P P(12,10,E)	8.71(2)	0.0507(2)	0.0588		0.643(1)	-0.00110(0)			
1096.378207(12)	10	7	E	11	8	E	^P P(11,8,E)	13.36(2)	0.0522(2)	0.0582	0.677(15)	0.645(1)	-0.00340(15)			
1096.631621(5)	6	2	E	7	1	E	^R P(7,1,E)	15.86(2)	0.0632(1)	0.0626	0.822(4)	0.693(6)	-0.00160(14)	0.0846(6)	0.772(7)	
1096.879089(6)	9	5	A1	10	6	A2	^P P(10,6,A2)	35.63(3)	0.0545(1)	0.0569	0.762(5)	0.635(1)	-0.00271(6)	0.000012(1)	0.0777(8)	0.696(23)
1097.713516(7)	8	3	E	9	4	E	^P P(9,4,E)	19.9(2)	0.0574(1)	0.0578	0.801(6)	0.643(2)	-0.00264(11)	0.000013(1)	0.0788(9)	0.763(19)
1098.725853(5)	6	1	A1	7	0	A2	^R P(7,0,A2)	28.66(2)	0.0650(1)	0.0633	0.829(2)	0.701(6)	-0.00223(8)	0.000016(1)	0.0852(4)	0.788(4)
1098.933992(6)	7	1	E	8	2	E	^P P(8,2,E)	17.10(2)	0.0628(2)	0.0613	0.821(6)	0.681(4)	-0.00207(14)	0.000024(2)	0.0820(7)	0.784(12)
1099.005454(7)	5	4	A2	6	3	A1	^R P(6,3,A1)	7.32(1)	0.0693(3)	0.0643	0.804(6)	0.720(7)	-0.00294(20)	0.000051(5)	0.0894(13)	0.761(12)
1100.672437(8)	10	8	A2	11	9	A1	^P P(11,9,A1)	27.42(3)	0.0512(1)	0.0596	0.750(8)	0.656(1)	-0.00255(8)	0.000024(2)	0.0767(6)	
1100.743446(20)	11	10	E	12	11	E	^P P(12,11,E)	8.80(2)	0.0434(2)	0.0589	0.660(29)	0.645(1)	-0.00262(18)			
1100.921805(8)	9	6	E	10	7	E	^P P(10,7,E)	19.25(2)	0.0545(1)	0.0587	0.709(9)	0.653(2)	-0.00226(10)	0.000032(2)	0.0815(7)	
1101.505850(6)	8	4	E	9	5	E	^P P(9,5,E)	23.28(2)	0.0569(1)	0.0577	0.775(6)	0.641(2)	-0.00247(9)	0.000021(2)	0.0787(8)	0.771(18)
1101.981493(6)	5	3	E	6	2	E	^R P(6,2,E)	7.95(1)	0.0642(2)	0.0633	0.834(5)	0.699(6)		0.0885(5)		
1102.423989(4)	7	2	A2	8	3	A1	^P P(8,3,A1)	22.84(1)	0.0655(2)	0.0600	0.779(8)	0.666(4)	-0.00215(7)	0.000025(1)	0.0859(2)	0.796(26)
1102.468792(4)	7	2	A1	8	3	A2	^P P(8,3,A2)	22.84(1)	0.0655(2)	0.0600	0.779(8)	0.666(4)	-0.00215(7)	0.000025(1)	0.0859(2)	0.796(26)
1103.850673(6)	6	0	E	7	1	E	^P P(7,1,E)	13.84(2)	0.0655(2)	0.0633	0.816(5)	0.701(6)	-0.00189(17)	0.000021(3)	0.0890(8)	0.750(8)
1105.032601(5)	5	2	E	6	1	E	^R P(6,1,E)	15.20(2)	0.0645(2)	0.0639	0.832(3)	0.703(6)	-0.00276(16)	0.00861(6)	0.767(6)	
1105.115847(14)	9	7	E	10	8	E	^P P(10,8,E)	20.64(4)	0.0537(3)	0.0604	0.733(19)	0.669(2)	-0.00236(20)		0.912(25)	
1105.130058(21)	10	9	E	11	10	E	^P P(11,10,E)	14.16(4)	0.0480(3)	0.0599	0.716(37)	0.660(1)		0.0773(25)		

1105.447409(6)	8	5	A1	9	6	A2	^R P(9,6,A2)	52.73(4)	0.057(1)	0.0591	0.765(3)	0.659(3)	-0.00284(6)	0.000014(1)	0.0778(5)	0.804(11)	
1105.490676(14)	11	11	A1	12	12	A2	^R P(12,12,A2)	17.12(3)	0.0269(1)	0.0558	0.375(19)	0.634(1)	-0.00514(7)	0.000029(2)			
1106.132104(6)	7	3	E	8	4	E	^R P(8,4,E)	28.56(2)	0.0593(1)	0.0591	0.812(4)	0.653(3)	-0.0033(8)	0.000017(1)	0.0781(5)	0.809(9)	
1107.190909(20)	4	4	A1	5	3	A2	^R P(5,3,A2)	3.62(2)	0.0760(14)	0.0669		0.748(7)		0.000030(2)			
1107.196929(12)	6	1	E	7	2	E	^R P(7,2,E)	22.91(4)	0.0627(2)	0.0624	0.801(5)	0.691(6)	-0.00258(11)	0.000019(2)	0.0879(7)	0.738(7)	
1107.406665(5)	5	1	A2	6	0	A1	^R P(6,0,A1)	32.60(2)	0.0665(1)	0.0647	0.841(1)	0.711(6)	-0.00288(7)	0.000019(1)	0.0861(3)	0.775(3)	
1109.465904(7)	9	8	A1	10	9	A2	^R P(10,9,A2)	43.05(4)	0.0500(1)	0.0609	0.726(5)	0.676(2)	-0.00207(6)	0.000023(1)	0.0750(9)	0.753(26)	
1109.536457(7)	8	6	E	9	7	E	^R P(9,7,E)	29.08(4)	0.0565(1)	0.0610	0.768(6)	0.680(3)	-0.00218(9)	0.000019(2)	0.0788(8)	0.804(18)	
1109.761551(14)	10	10	E	11	11	E	^R P(11,11,E)	14.36(2)	0.0301(1)	0.0568	0.510(14)	0.647(1)	-0.00435(9)	0.000041(2)			
1109.967774(6)	7	4	E	8	5	E	^R P(8,5,E)	33.02(3)	0.0588(1)	0.0598	0.790(3)	0.664(3)	-0.00137(8)	0.000028(1)	0.0821(5)	0.761(8)	
1110.192698(6)	4	3	E	5	2	E	^R P(5,2,E)	5.81(1)	0.0741(2)	0.0654		0.724(6)	-0.00362(36)		0.0908(4)		
1110.754522(7)	6	2	A1	7	3	A2	^R P(7,3,A2)	30.93(1)	0.0645(1)	0.0612	0.805(1)	0.675(5)	-0.00218(4)	0.000026(1)	0.0871(1)	0.787(1)	
1110.779654(12)	6	2	A2	7	3	A1	^R P(7,3,A1)	30.93(1)	0.0645(1)	0.0612	0.805(1)	0.675(5)	-0.00218(4)	0.000026(1)	0.0871(1)	0.787(1)	
1111.988897(5)	5	0	E	6	1	E	^R P(6,1,E)	18.51(2)	0.0656(1)	0.0647	0.849(2)	0.711(6)	-0.00204(14)	0.000016(2)	0.0870(5)	0.772(5)	
1113.297730(5)	4	2	E	5	1	E	^R P(5,1,E)	12.88(2)	0.0645(2)	0.0655	0.861(2)	0.717(6)	-0.00314(17)		0.0896(6)	0.755(5)	
1113.776358(7)	8	7	E	9	8	E	^R P(9,8,E)	31.26(3)	0.0540(1)	0.0618	0.730(5)	0.691(4)	-0.00262(8)				
1113.948879(5)	7	5	A2	8	6	A1	^R P(8,6,A1)	75.51(5)	0.0594(1)	0.0616	0.781(2)	0.688(4)	-0.00259(6)	0.000009(1)	0.0803(3)	0.795(5)	
1113.979823(10)	9	9	E	10	10	E	^R P(10,10,E)	22.52(5)	0.0342(1)	0.0578	0.534(12)	0.660(1)	-0.00467(9)	0.000031(2)	0.0539(19)	0.669(65)	
1114.493311(5)	6	3	E	7	4	E	^R P(7,4,E)	38.27(2)	0.0609(1)	0.0609	0.816(2)	0.672(4)	-0.00270(7)	0.000015(1)	0.0816(3)	0.779(4)	
1115.420049(5)	5	1	E	6	2	E	^R P(6,2,E)	29.34(2)	0.0634(1)	0.0638	0.835(2)	0.701(6)	-0.00214(8)	0.000021(1)	0.0848(4)	0.786(4)	
1115.940928(5)	4	1	A1	5	0	A2	^R P(5,0,A1)	33.58(2)	0.0669(1)	0.0663	0.856(1)	0.723(6)	-0.00241(8)	0.000011(1)	0.0878(3)	0.774(3)	
1118.076223(5)	7	6	E	8	7	E	^R P(8,7,E)	41.80(3)	0.0568(1)	0.0627	0.760(3)	0.703(5)	-0.00215(6)	0.000014(1)	0.0793(4)	0.766(9)	
1118.172377(5)	8	8	A1	9	9	A2	^R P(9,9,A2)	65.54(3)	0.0385(0)	0.0588	0.547(3)	0.675(2)	-0.00374(3)	0.000033(1)	0.0588(5)	0.697(16)	
1118.304501(7)	3	3	E	4	2	E	^R P(4,2,E)	2.87(0)	0.0782(10)	0.0677	0.770(15)	0.749(7)	-0.00730(61)		0.0873(26)	0.806(23)	
1118.363421(4)	6	4	E	7	5	E	^R P(7,5,E)	45.26(3)	0.0610(1)	0.0623	0.822(3)	0.694(5)	-0.00233(6)	0.000015(1)	0.0838(3)	0.773(4)	
1119.025382(8)	5	2	A2	6	3	A1	^R P(6,3,A1)	40.05(1)	0.0675(0)	0.0627	0.814(1)	0.688(5)	-0.00210(3)	0.000023(2)	0.0925(1)	0.761(1)	
1119.038034(12)	5	2	A1	6	3	A2	^R P(6,3,A2)	40.05(1)	0.0675(0)	0.0627	0.814(1)	0.688(5)	-0.00210(3)	0.000023(2)	0.0925(1)	0.761(1)	
1120.103181(4)	4	0	E	5	1	E	^R P(5,1,E)	22.67(2)	0.0663(1)	0.0663	0.850(2)	0.722(6)	-0.00250(11)	0.000013(1)	0.0887(4)	0.761(3)	
1121.441410(5)	3	2	E	4	1	E	^R P(4,1,E)	9.24(1)	0.0662(2)	0.0671	0.853(4)	0.734(6)	-0.00233(14)		0.0911(8)	0.739(6)	
1122.353699(6)	7	7	E	8	8	E	^R P(8,8,E)	44.77(7)	0.0426(1)	0.0599	0.629(6)	0.690(3)	-0.00319(8)	0.000026(1)	0.0638(5)	0.745(14)	
1122.376165(4)	6	5	A2	7	6	A1	^R P(7,6,A1)	105.06(7)	0.0604(1)	0.0636	0.789(2)	0.714(6)	-0.00207(5)	0.000017(1)	0.0806(2)	0.784(3)	
1122.788184(4)	5	3	E	6	4	E	^R P(6,4,E)	49.73(2)	0.0634(1)	0.0631	0.825(2)	0.699(5)	-0.00273(5)	0.000010(1)	0.0835(3)	0.781(3)	
1123.589807(4)	4	1	E	5	2	E	^R P(5,2,E)	35.43(2)	0.0640(1)	0.0652	0.842(2)	0.713(6)	-0.00308(7)	0.000014(1)	0.0857(3)	0.772(3)	
1124.325714(4)	3	1	A2	4	0	A1	^R P(4,0,A1)	31.36(2)	0.0673(1)	0.0679	0.860(1)	0.735(6)	-0.00284(8)	0.000010(1)	0.0896(3)	0.765(3)	
1126.534176(6)	6	6	E	7	7	E	^R P(7,7,E)	58.571(4)	0.0488(1)	0.0611	0.680(2)	0.704(5)	-0.00313(4)	0.000030(1)	0.0706(6)	0.668(18)	
1126.684492(6)	5	4	E	6	5	E	^R P(6,5,E)	59.77(3)	0.0623(1)	0.0645	0.805(2)	0.721(6)	-0.00243(5)	0.000009(1)	0.0807(6)	0.871(18)	
1127.227037(20)	4	2	A1	5	3	A2	^R P(5,3,A2)	48.64(1)	0.0643(0)	0.0645	0.822(1)	0.709(6)	-0.00251(4)	0.000015(2)	0.0737(9)		
1127.232695(14)	4	2	A2	5	3	A1	^R P(5,3,A1)	48.64(1)	0.0643(0)	0.0645	0.822(1)	0.709(6)	-0.00251(4)	0.000015(2)	0.0737(9)		
1128.174506(6)	3	0	E	4	1	E	^R P(4,1,E)	25.18(2)	0.0674(1)	0.0679	0.836(2)	0.734(6)	-0.00224(10)	0.000013(1)	0.0839(2)		
1129.139102(28)	10	9	E	10	8	E	^R Q(10,8,E)	3.84(1)	0.0615(5)	0.0611		0.684(4)	-0.00498(40)				
1129.476960(11)	2	2	E	3	1	E	^R P(3,1,E)	4.62(1)	0.0762(3)	0.0689		0.753(7)	-0.00189(17)				
1130.486989(25)	11	8	E	11	7	E	^R Q(11,7,E)	4.89(2)	0.0558(5)	0.0576		0.522(43)	0.644(1)				
1130.561033(30)	13	7	A2	13	6	A1	^R Q(13,6,A1)	5.63(2)	0.0509(4)	0.0532		0.549(51)	0.605(1)	0.000065(6)			
1130.721975(5)	5	5	A2	6	6	A1	^R P(6,6,A1)	140.05(4)	0.0537(1)	0.0623		0.724(1)	0.716(5)	-0.00289(3)	0.000024(2)	0.0707(3)	0.806(11)
1131.008024(20)	4	3	E	5	4	E	^R P(5,4,E)	62.37(2)	0.0647(1)	0.0653		0.822(1)	0.728(6)	-0.00228(6)	0.000010(1)	0.0837(6)	0.828(17)
1131.434300(19)	10	8	E	10	7	E	^R Q(10,7,E)	6.00(2)	0.0597(4)	0.0598		0.558(29)	0.669(3)	-0.00477(38)			
1131.693962(6)	3	1	E	4	2	E	^R P(4,2,E)	40.36(2)	0.0644(1)	0.0668		0.846(1)	0.727(6)	-0.00292(7)	0.000014(1)	0.0836(9)	0.818(24)
1131.766548(18)	12	7	A2	12	6	A1	^R Q(12,6,A1)	8.54(2)	0.0521(3)	0.0543		0.748(31)	0.614(1)	-0.00291(25)			
1132.557787(6)	2	1	A1	3	0	A2	^R P(3,0,A2)	24.95(2)	0.0667(1)	0.0695		0.869(2)	0.749(6)	-0.00335(16)	0.000012(1)	0.0919(2)	
1132.858722(13)	11	7	A2	11	6	A1	^R Q(11,6,A1)	12.16(3)	0.0561(5)	0.0559		0.582(26)	0.629(1)				
1133.033465(17)	8	8	E	8	7	E	^R Q(8,7,E)	4.79(1)	0.0695(5)	0.0628		0.719(6)	-0.00978(64)				
1133.841173(10)	10	7	A2	10	6	A1	^R Q(10,6,A1)	15.93(3)	0.0571(3)	0.0580		0.714(16)	0.650(2)				
1134.717981(8)	9	7	A1	9	6	A2	^R Q(9,6,A2)	19.06(3)	0.0597(3)	0.0603		0.748(11)	0.677(3)				
1134.923731(6)	4	4	E	5	5	E	^R P(5,5,E)	76.54(3)	0.0582(1)	0.0635		0.747(2)	0.727(6)	-0.00182(7)	0.000027(1)	0.0354(7)	

Table 5 (continued)

Position, cm ⁻¹	J	K'	S'	J''	K''	S''	Assignment	Int*10 ^{25a}	$b_L^0(N_2)$ expt, ^b	$b_L^0(N_2)$ calc. ^b	n_1 expt	n_1 calc.	$\delta^0(N_2)$ expt ^b	$\delta'(N_2)$ expt ^c	$b_L^0(self)$ expt ^b	n_2 expt
1135.352143(22)	3	2	A2	4	3	A1	^p P(4,3,A1)	114.47(3)	0.0653(1)	0.0664	0.852(1)	0.733(6)	-0.00225(13)	0.000012(1)	0.0857(1)	
1135.493275(8)	8	7	A2	8	6	A1	^R Q(8,6,A1)	19.18(5)	0.0628(3)	0.0626	0.821(10)	0.705(5)	-0.0036(36)		0.0841(6)	
1136.171086(19)	7	7	A1	7	6	A2	^R Q(7,6,A2)	14.28(5)	0.0697(6)	0.0638	0.764(17)	0.728(7)			0.0868(16)	
1136.185383(14)	2	0	E	3	1	E	^p P(3,1,E)	25.02(2)	0.0668(2)	0.0695	0.855(3)	0.748(6)			0.0910(5)	
1136.350725(13)	10	6	E	10	5	E	^R Q(10,5,E)	9.78(2)	0.0572(5)	0.0563	0.642(25)	0.633(1)				
1137.263915(10)	9	6	E	9	5	E	^R Q(9,5,E)	12.53(2)	0.0585(4)	0.0584	0.818(16)	0.655(2)				
1137.869412(20)	11	5	E	11	4	E	^R Q(11,4,E)	7.64(2)	0.0546(3)	0.0550	0.739(23)	0.620(1)			0.0753(25)	
1138.068790(9)	8	6	E	8	5	E	^R Q(8,5,E)	14.15(2)	0.0620(1)	0.0608		0.683(4)	-0.00187(13)		0.0869(6)	
1138.770173(8)	7	6	E	7	5	E	^R Q(7,5,E)	14.16(2)	0.0664(1)	0.0633		0.712(6)	-0.00255(13)	0.000020(1)	0.0874(5)	
1138.949449(13)	10	5	E	10	4	E	^R Q(10,4,E)	11.08(2)	0.0574(2)	0.0559	0.651(14)	0.628(1)			0.0795(14)	
1139.112237(35)	3	3	E	4	4	E	^p P(4,4,E)	4.81(2)	0.0529(4)	0.0649	0.830(8)	0.737(6)				
1139.372679(12)	6	6	E	6	5	E	^R Q(6,5,E)	9.95(2)	0.0679(3)	0.0647	0.844(7)	0.735(7)	-0.00491(26)	0.000042(4)	0.096(13)	0.707(12)
1139.722075(6)	2	1	E	3	2	E	^p P(3,2,E)	43.46(2)	0.0649(1)	0.0682	0.854(1)	0.745(6)	-0.00203(6)	0.000022(1)	0.0883(1)	
1139.909156(11)	9	5	E	9	4	E	^R Q(9,4,E)	14.64(2)	0.0578(2)	0.0572	0.716(9)	0.639(1)			0.0866(8)	
1140.391680(21)	11	4	A1	11	3	A2	^R Q(11,3,A2)	7.11(2)	0.0602(4)	0.0559	0.760(35)	0.628(1)	0.00427(41)		0.0850(27)	
1140.427310(20)	11	4	A2	11	3	A1	^R Q(11,3,A1)	7.50(2)	0.0598(4)	0.0559	0.707(33)	0.628(1)	-0.00522(38)		0.0848(26)	
1140.634587(6)	1	1	A2	2	0	A1	^R P(2,0,A1)	14.39(1)	0.0664(1)	0.0710	0.839(2)	0.764(6)	-0.00318(15)	0.000024(1)	0.0919(1)	
1140.752289(8)	8	5	E	8	4	E	^R Q(8,4,E)	18.20(2)	0.0603(1)	0.0590		0.659(3)	-0.00082(8)		0.0819(4)	
1141.483940(6)	7	5	E	7	4	E	^R Q(7,4,E)	20.29(3)	0.0638(1)	0.0615	0.786(4)	0.687(5)	-0.00220(13)	0.000011(1)	0.0866(3)	
1141.562032(14)	10	4	A2	10	3	A1	^R Q(10,3,A1)	10.67(2)	0.0623(3)	0.0566	0.699(21)	0.635(1)				
1141.597406(13)	10	4	A1	10	3	A2	^R Q(10,3,A2)	11.42(2)	0.0598(3)	0.0566	0.780(19)	0.635(1)	-0.00574(26)			
1142.109752(6)	6	5	E	6	4	E	^R Q(6,4,E)	19.43(2)	0.0663(1)	0.0640	0.819(4)	0.718(6)	-0.00323(12)	0.000016(2)	0.0909(3)	
1142.582166(11)	9	4	A1	9	3	A2	^R Q(9,3,A2)	14.07(3)	0.0634(2)	0.0575	0.801(9)	0.642(2)	0.00366(9)		0.0819(13)	0.850(19)
1142.628435(19)	9	4	A2	9	3	A1	^R Q(9,3,A1)	15.86(6)	0.0634(2)	0.0575	0.801(9)	0.642(2)	0.00366(9)		0.0819(13)	0.850(19)
1142.635080(9)	5	5	E	5	4	E	^R Q(5,4,E)	13.68(4)	0.0680(3)	0.0657	0.87(8)	0.742(7)	-0.01596(25)		0.0935(4)	
1143.391181(6)	2	2	A1	3	3	A2	^p P(3,3,A2)	131.69(3)	0.0656(0)	0.0665	0.832(1)	0.746(6)	-0.00248(4)	0.000017(2)	0.0853(2)	0.787(2)
1143.527523(7)	8	4	A1	8	3	A2	^R Q(8,3,A2)	20.88(2)	0.0653(1)	0.0586	0.785(3)	0.652(3)	-0.00174(6)		0.0878(2)	
1143.571633(8)	8	4	A2	8	3	A1	^R Q(8,3,A1)	19.27(3)	0.0653(1)	0.0586	0.785(3)	0.652(3)	-0.00174(6)		0.0878(2)	
1144.121476(6)	1	0	E	2	1	E	^p P(2,1,E)	22.36(2)	0.0662(1)	0.0709	0.861(2)	0.763(6)	-0.0029(10)	0.000020(1)	0.0924(4)	0.741(4)
1144.218243(14)	10	3	E	10	2	E	^R Q(10,2,E)	9.88(2)	0.0602(3)	0.0578	0.829(18)	0.646(1)	-0.00249(24)			
1144.302129(14)	7	4	A2	7	3	A1	^R Q(7,3,A1)	25.11(2)	0.0619(1)	0.0602	0.811(1)	0.667(4)	-0.00107(5)	0.000007(1)	0.0838(6)	0.762(5)
1144.307543(14)	7	4	A1	7	3	A2	^R Q(7,3,A2)	25.11(2)	0.0619(1)	0.0602	0.811(1)	0.667(4)	-0.00107(5)	0.000007(1)	0.0838(6)	0.762(5)
1144.960509(50)	6	4	A1	6	3	A2	^R Q(6,3,A2)	54.31(3)	0.0641(1)	0.0624	0.825(2)	0.692(6)	-0.00170(5)		0.0873(5)	0.816(12)
1145.360462(8)	9	3	E	9	2	E	^R Q(9,2,E)	14.55(3)	0.0607(2)	0.0586	0.756(9)	0.655(2)	-0.00201(15)		0.0841(7)	
1145.508861(5)	5	4	A2	5	3	A1	^R Q(5,3,A1)	50.63(2)	0.0671(1)	0.0648	0.842(1)	0.722(6)	-0.00221(6)	0.000015(1)	0.0908(2)	
1145.955000(5)	4	4	A1	4	3	A2	^R Q(4,3,A2)	34.56(2)	0.0705(1)	0.0668	0.864(1)	0.747(7)	-0.00373(8)	0.000024(1)	0.0956(2)	
1146.350463(6)	8	3	E	8	2	E	^R Q(8,2,E)	20.22(2)	0.0591(1)	0.0595	0.812(5)	0.663(3)	-0.00155(10)		0.0862(4)	
1146.564067(18)	10	2	E	10	1	E	^R Q(10,1,E)	5.12(1)	0.0618(4)	0.0587	0.813(28)	0.655(2)				
1147.196047(6)	7	3	E	7	2	E	^R Q(7,2,E)	26.37(2)	0.0606(1)	0.0607	0.813(3)	0.672(4)	-0.00073(6)	0.000011(1)	0.0850(3)	
1147.665833(5)	1	1	E	2	2	E	^p P(2,2,E)	45.26(2)	0.0665(1)	0.0684	0.859(1)	0.757(6)	-0.00221(6)	0.000017(1)	0.0933(5)	0.755(10)
1147.906526(8)	6	3	E	6	2	E	^R Q(6,2,E)	32.07(3)	0.0633(1)	0.0621	0.834(3)	0.684(5)			0.0893(10)	0.703(20)
1148.492390(5)	5	3	E	5	2	E	^R Q(5,2,E)	33.82(2)	0.0651(1)	0.0639	0.832(2)	0.703(6)	-0.00182(7)	0.000009(1)	0.0868(2)	
1148.963335(5)	4	3	E	4	2	E	^R Q(4,2,E)	30.82(2)	0.0666(1)	0.0660	0.849(2)	0.728(6)	-0.00184(8)	0.000014(1)	0.0897(2)	
1149.063784(7)	8	2	E	8	1	E	^R Q(8,1,E)	13.87(2)	0.0644(2)	0.0607	0.780(8)	0.677(4)			0.0879(6)	
1149.328536(5)	3	3	E	3	2	E	^R Q(3,2,E)	20.75(2)	0.0697(1)	0.0678	0.873(2)	0.752(6)	-0.00275(12)	0.000018(1)	0.0956(3)	
1150.055828(6)	7	2	E	7	1	E	^R Q(7,1,E)	20.49(2)	0.0631(1)	0.0618	0.839(4)	0.686(5)			0.000011(2)	0.0866(3)
1150.8805049(5)	6	2	E	6	1	E	^R Q(6,1,E)	27.63(2)	0.0633(1)	0.0631	0.835(2)	0.696(6)	-0.00147(8)		0.0883(2)	
1151.547989(5)	5	2	E	5	1	E	^R Q(5,1,E)	33.79(2)	0.0645(1)	0.0646	0.83(2)	0.707(6)	-0.00158(7)		0.0881(2)	
1151.972417(6)	0	0	E	1	1	E	^p P(1,1,E)	16.39(2)	0.0657(1)	0.0720	0.834(2)	0.773(6)	-0.00267(13)	0.000021(1)	0.0957(3)	

1152.072139(5)	4	2	E	4	1	E	^R Q(4,1,E)	36.78(2)	0.0649(1)	0.0662	0.855(1)	0.721(6)	-0.00191(7)	0.0883(2)		
1152.468500(5)	3	2	E	3	1	E	^R Q(3,1,E)	33.77(2)	0.0653(1)	0.0678	0.850(1)	0.739(6)	-0.00241(7)	0.000014(1)	0.0889(2)	
1152.751674(5)	2	2	E	2	1	E	^R Q(2,1,E)	22.87(1)	0.0663(1)	0.0692	0.864(1)	0.757(6)	-0.0023(10)	0.000019(1)	0.0930(2)	
1154.43943(16)	13	1	A1	13	0	A2	^R Q(13,0,A2)	15.64(3)	0.0590(2)	0.0564	0.84(19)	0.623(1)	-0.00186(12)	0.000018(3)	0.0891(21)	
1154.713917(12)	12	1	A2	12	0	A1	^R Q(12,0,A1)	22.1(3)	0.0591(2)	0.0573	0.87(12)	0.634(1)	-0.00135(11)	0.0661(9)		
1154.966470(9)	11	1	A1	11	0	A2	^R Q(11,0,A2)	32.63(5)	0.0603(1)	0.0582	0.769(7)	0.646(1)	-0.00158(9)	0.000013(2)	0.0843(6)	
1155.070691(21)	13	0	E	13	1	E	^P Q(13,1,E)	10.78(3)	0.0606(3)	0.0564	0.634(30)	0.623(1)		0.0774(28)		
1155.199670(8)	10	1	A2	10	0	A1	^R Q(10,0,A1)	44.83(4)	0.0618(1)	0.0592	0.776(4)	0.659(2)	-0.00110(7)	0.000016(1)	0.0826(4)	
1155.422423(7)	9	1	A1	9	0	A2	^R Q(9,0,A2)	55.81(5)	0.0625(1)	0.0603	0.790(3)	0.672(3)	-0.00116(7)	0.0833(3)		
1155.521843(7)	8	1	A2	8	0	A1	^R Q(8,0,A1)	64.88(5)	0.0650(1)	0.0614	0.822(3)	0.684(4)	-0.00267(7)	0.000018(1)	0.0855(3)	
1155.594148(12)	12	0	E	12	1	E	^P Q(12,1,E)	21.25(4)	0.0601(2)	0.0573	0.768(17)	0.634(1)	-0.00133(10)	0.0806(12)		
1155.728731(7)	7	1	A1	7	0	A2	^R Q(7,0,A2)	89.9(5)	0.0649(1)	0.0626	0.824(2)	0.695(5)	-0.00203(5)	0.000016(1)	0.0851(2)	
1155.879355(7)	6	1	A2	6	0	A1	^R Q(6,0,A1)	102.37(6)	0.0655(1)	0.0639	0.831(1)	0.705(6)	-0.00146(6)	0.000013(1)	0.0860(2)	
1156.004835(13)	5	1	A1	5	0	A2	^R Q(5,0,A2)	107.72(10)	0.0659(1)	0.0654	0.828(1)	0.715(6)	-0.00186(6)	0.000007(1)	0.0841(3)	
1156.108549(7)	4	1	A2	4	0	A1	^R Q(4,0,A1)	107.76(7)	0.0660(1)	0.0670	0.855(1)	0.727(6)	-0.00206(6)	0.000005(1)	0.0872(2)	
1156.191028(7)	3	1	A1	3	0	A2	^R Q(3,0,A2)	97.04(8)	0.0660(1)	0.0687	0.840(2)	0.740(6)	-0.00190(7)	0.0876(2)		
1156.252680(8)	2	1	A2	2	0	A1	^R Q(2,0,A1)	77.66(9)	0.0666(1)	0.0702	0.820(2)	0.755(6)	-0.00248(9)	0.000009(1)	0.0869(8)	0.814(20)
1156.293622(11)	1	1	A1	1	0	A2	^R Q(1,0,A2)	49.68(7)	0.0671(1)	0.0716	0.758(2)	0.770(6)	-0.00354(9)	0.000014(1)	0.0892(3)	
1156.424297(8)	10	0	E	10	1	E	^P Q(10,1,E)	39.85(4)	0.0614(1)	0.0592	0.802(6)	0.659(2)	-0.00164(7)	0.0830(4)		
1156.658762(37)	14	1	E	14	2	E	^P Q(14,2,E)	8.40(4)	0.0582(3)	0.0553		0.612(1)		0.0794(46)		
1156.836955(8)	9	0	E	9	1	E	^P Q(9,1,E)	50.63(4)	0.0623(1)	0.0603	0.804(3)	0.672(3)	-0.00168(6)	0.000007(1)	0.0836(3)	
1157.255809(11)	8	0	E	8	1	E	^P Q(8,1,E)	60.80(7)	0.0632(1)	0.0614	0.807(3)	0.684(4)	-0.0016(10)	0.0849(3)		
1157.272717(28)	13	1	E	13	2	E	^P Q(13,2,E)	13.02(5)	0.0612(4)	0.0561	0.865(50)	0.622(1)		0.0783(36)		
1157.679116(7)	7	0	E	7	1	E	^P Q(7,1,E)	68.21(4)	0.0646(1)	0.0626	0.815(2)	0.695(5)	-0.00171(5)	0.000010(1)	0.0802(8)	0.883(24)
1157.885570(41)	12	1	E	12	2	E	^P Q(12,2,E)	18.58(3)	0.0596(2)	0.0569	0.720(14)	0.631(1)	-0.00221(14)			
1158.099455(8)	6	0	E	6	1	E	^P Q(6,1,E)	71.64(4)	0.0657(1)	0.0639	0.807(2)	0.705(6)	-0.00196(5)	0.000008(1)	0.0810(9)	0.898(25)
1158.504362(9)	5	0	E	5	1	E	^P Q(5,1,E)	71.38(3)	0.0690(1)	0.0654	0.792(1)	0.715(6)	-0.00186(5)	0.000007(1)	0.0821(12)	0.877(33)
1158.877568(7)	4	0	E	4	1	E	^P Q(4,1,E)	64.98(3)	0.0663(1)	0.0670	0.839(1)	0.727(6)	-0.00183(5)	0.0826(9)	0.882(24)	
1159.116825(9)	10	1	E	10	2	E	^P Q(10,2,E)	34.05(5)	0.0612(1)	0.0587	0.770(7)	0.655(2)	-0.00248(9)	0.000022(2)	0.0792(4)	
1159.201560(8)	3	0	E	3	1	E	^P Q(3,1,E)	54.72(3)	0.0662(1)	0.0687	0.840(1)	0.740(6)	-0.00226(6)	0.000013(1)	0.0879(2)	
1159.460170(8)	2	0	E	2	1	E	^P Q(2,1,E)	41.65(2)	0.0664(1)	0.0702	0.840(1)	0.755(6)	-0.00236(7)	0.0883(2)		
1159.513193(34)	14	2	A2	14	3	A1	^P Q(14,3,A1)	7.37(3)	0.0572(4)	0.0549	0.697(56)	0.610(1)		0.0672(45)		
1159.640105(8)	1	0	E	1	1	E	^P Q(1,1,E)	25.71(2)	0.0668(1)	0.0716	0.832(1)	0.770(6)	-0.00377(13)	0.000026(1)	0.0937(22)	0.656(53)
1159.728243(8)	9	1	E	9	2	E	^P Q(9,2,E)	41.49(4)	0.0604(1)	0.0597	0.827(4)	0.666(3)	-0.00260(7)	0.000021(1)	0.0876(13)	0.670(34)
1159.810303(21)	13	2	A2	13	3	A1	^P Q(13,3,A1)	11.23(3)	0.0604(3)	0.0555	0.924(31)	0.619(1)				
1160.326721(7)	8	1	E	8	2	E	^P Q(8,2,E)	49.84(4)	0.0618(1)	0.0607	0.805(2)	0.677(4)	-0.00244(6)	0.000014(1)	0.0840(2)	
1160.638984(13)	12	2	A1	12	3	A2	^P Q(12,3,A2)	16.19(2)	0.0611(1)	0.0562		0.627(1)		0.0852(12)		
1160.901607(7)	7	1	E	7	2	E	^P Q(7,2,E)	56.15(3)	0.0627(1)	0.0618	0.813(2)	0.686(5)	-0.00259(6)	0.000015(1)	0.0839(2)	
1160.958662(14)	12	2	A2	12	3	A1	^P Q(12,3,A1)	16.19(2)	0.0611(1)	0.0562		0.627(1)		0.0852(12)		
1161.440596(8)	6	1	E	6	2	E	^P Q(6,2,E)	59.47(3)	0.0640(1)	0.0631	0.818(2)	0.696(6)	-0.00153(6)	0.000018(1)	0.0858(2)	
1161.685867(9)	10	4	E	10	5	E	^P Q(10,5,E)	22.04(3)	0.0617(2)	0.0559	0.766(9)	0.628(1)	-0.00299(13)	0.000041(3)	0.0871(8)	
1161.930961(6)	5	1	E	5	2	E	^P Q(5,2,E)	58.61(2)	0.0645(1)	0.0646	0.833(1)	0.707(6)	-0.00229(6)	0.000014(1)	0.0811(8)	0.907(23)
1162.239713(9)	10	2	A1	10	3	A2	^P Q(10,3,A2)	29.52(3)	0.0628(1)	0.0578	0.787(4)	0.646(1)	-0.00217(7)	0.0828(4)		
1162.360469(7)	4	1	E	4	2	E	^P Q(4,2,E)	53.94(3)	0.0649(1)	0.0662	0.860(1)	0.721(6)	-0.00289(6)	0.000010(1)	0.0869(2)	
1162.406376(8)	10	2	A2	10	3	A1	^P Q(10,3,A1)	29.52(3)	0.0628(1)	0.0578	0.787(4)	0.646(1)	-0.00217(7)	0.0839(2)		
1162.718028(7)	3	1	E	3	2	E	^P Q(3,2,E)	43.17(2)	0.0660(1)	0.0678	0.857(1)	0.739(6)	-0.00155(7)	0.000013(1)	0.0878(2)	
1162.994624(9)	2	1	E	2	2	E	^P Q(2,2,E)	26.68(2)	0.0672(1)	0.0692	0.871(2)	0.757(7)		0.000020(1)	0.0909(4)	
1162.997143(10)	9	2	A2	9	3	A1	^P Q(9,3,A1)	36.84(5)	0.0639(1)	0.0586	0.778(2)	0.655(2)	-0.00124(4)	0.000014(1)	0.0878(2)	
1163.110746(7)	9	2	A1	9	3	A2	^P Q(9,3,A2)	35.93(5)	0.0639(1)	0.0586	0.778(2)	0.655(2)	-0.00124(4)	0.000014(1)	0.0878(2)	
1163.474647(54)	2	1	A1	1	0	A2	^R (1,0,A2)	0.56(0)	0.0768(15)							
1163.714357(8)	8	2	A1	8	3	A2	^P Q(8,3,A2)	43.63(3)	0.0645(1)	0.0595	0.826(2)	0.663(3)	-0.00212(4)	0.000026(1)	0.0869(1)	
1163.787924(8)	8	2	A2	8	3	A1	^P Q(8,3,A1)	42.83(4)	0.0645(1)	0.0595	0.826(2)	0.663(3)	-0.00212(4)	0.000026(1)	0.0869(1)	
1163.913919(7)	1	1	A2	0	0	A1	^R (0,0,A1)	35.40(2)	0.0646(1)		0.786(2)	-0.00096(8)	0.000007(1)	0.0913(14)	0.749(33)	
1164.049765(15)	12	3	E	12	4	E	^P Q(12,4,E)	14.48(4)	0.0559(2)	0.0553	0.621(1)	-0.00255(16)	0.0768(16)			

Table 5 (continued)

Position, cm ⁻¹	J	K'	S'	J''	K''	S''	Assignment	Int*10 ^{25a}	$b_L^0(N_2)$ expt, ^b	$b_L^0(N_2)$ calc. ^b	n_1 expt	n_1 calc.	$\delta^0(N_2)$ expt ^b	$\delta'(N_2)$ expt ^c	$b_L^0(self)$ expt ^b	n_2 expt	
1164.381569(5)	7	2	A2	7	3	A1	^p Q(7,3,A1)	48.71(4)	0.0672(1)	0.0607	0.828(2)	0.672(4)	-0.00239(3)	0.000024(2)	0.0876(4)	0.750(13)	
1164.426483(5)	7	2	A1	7	3	A2	^p Q(7,3,A2)	47.97(5)	0.0672(1)	0.0607	0.828(2)	0.672(4)	-0.00239(3)	0.000024(2)	0.0876(4)		
1164.934109(10)	11	3	E	11	4	E	^p Q(11,4,E)	19.32(4)	0.0553(2)	0.0559	0.902(15)	0.628(1)				0.0955(33)	
1164.989362(4)	6	2	A1	6	3	A2	^p Q(6,3,A2)	50.48(1)	0.0696(1)	0.0621	0.843(2)	0.685(5)	-0.00232(3)	0.000025(2)	0.0906(1)	0.715(1)	
1165.014728(4)	6	2	A2	6	3	A1	^p Q(6,3,A1)	50.48(1)	0.0696(1)	0.0621	0.843(2)	0.685(5)	-0.00232(3)	0.000025(2)	0.0906(1)	0.715(1)	
1165.528810(6)	5	2	A2	5	3	A1	^p Q(5,3,A1)	48.03(1)	0.0641(0)	0.0639	0.845(1)	0.703(6)	-0.00205(4)	0.000015(2)	0.0896(2)		
1165.541406(6)	5	2	A1	5	3	A2	^p Q(5,3,A2)	48.03(1)	0.0641(0)	0.0639	0.845(1)	0.703(6)	-0.00205(4)	0.000015(2)	0.0896(2)		
1165.788102(8)	10	3	E	10	4	E	^p Q(10,4,E)	25.47(4)	0.0570(1)	0.0566	0.737(7)	0.635(1)	-0.00289(11)	0.000026(2)	0.0788(5)		
1165.991512(12)	4	2	A1	4	3	A2	^p Q(4,3,A2)	40.25(1)	0.0667(0)	0.0660	0.853(0)	0.728(6)	-0.00141(4)	0.000010(2)	0.0891(2)		
1165.996906(12)	4	2	A2	4	3	A1	^p Q(4,3,A1)	40.25(1)	0.0667(0)	0.0660	0.853(0)	0.728(6)	-0.00141(4)	0.000010(2)	0.0891(2)		
1166.370334(12)	3	2	A2	3	3	A1	^p Q(3,3,A1)	25.32(1)	0.0703(1)	0.0678	0.864(1)	0.751(7)		0.000005(2)	0.0927(2)		
1166.508093(33)	13	4	E	13	5	E	^p Q(13,5,E)	8.56(6)	0.0536(3)	0.0539		0.609(1)			0.0711(36)		
1166.602608(7)	9	3	E	9	4	E	^p Q(9,4,E)	30.78(4)	0.0566(1)	0.0575	0.796(5)	0.642(2)	-0.00242(9)	0.000026(2)	0.0824(4)		
1167.368139(6)	8	3	E	8	4	E	^p Q(8,4,E)	36.36(3)	0.0586(1)	0.0586	0.799(3)	0.652(3)	-0.00315(7)	0.000012(1)	0.0820(2)		
1167.522215(12)	12	4	E	12	5	E	^p Q(12,5,E)	12.37(2)	0.0535(2)	0.0544	0.695(17)	0.614(1)	-0.00321(16)				
1168.075586(6)	7	3	E	7	4	E	^p Q(7,4,E)	39.93(3)	0.0613(1)	0.0602	0.796(3)	0.667(4)	-0.00246(7)	0.000018(1)			
1168.270282(5)	2	2	E	1	1	E	^R R(1,1,E)	51.87(2)	0.0654(1)	0.0684	0.844(1)	0.757(6)	-0.00139(5)		0.0881(0)		
1168.500905(9)	11	4	E	11	5	E	^p Q(11,5,E)	16.89(2)	0.0549(1)	0.0550	0.709(11)	0.620(1)	-0.00322(13)	0.000021(3)			
1168.715933(5)	6	3	E	6	4	E	^p Q(6,4,E)	39.82(2)	0.0639(1)	0.0624	0.828(2)	0.692(6)	-0.00242(7)				
1168.909810(22)	14	5	A1	14	6	A2	^p Q(14,6,A2)	9.98(2)	0.0517(2)	0.0528	0.512(28)	0.601(2)	-0.00303(19)		0.0688(30)		
1169.280994(5)	5	3	E	5	4	E	^p Q(5,4,E)	34.79(2)	0.0671(1)	0.0648	0.849(2)	0.722(6)	-0.00152(8)		0.0880(2)		
1169.435777(7)	10	4	E	10	5	E	^p Q(10,5,E)	21.72(3)	0.0556(1)	0.0559	0.733(8)	0.628(1)	-0.00389(11)				
1169.763499(6)	4	3	E	4	4	E	^p Q(4,4,E)	22.23(2)	0.0700(1)	0.0668	0.861(2)	0.747(7)	-0.00187(11)		0.0931(2)		
1170.060167(13)	13	5	A2	13	6	A1	^p Q(13,6,A1)	14.88(2)	0.0514(2)	0.0532	0.686(16)	0.605(1)	-0.00345(13)				
1170.318393(6)	9	4	E	9	5	E	^p Q(9,5,E)	26.23(2)	0.0566(1)	0.0572	0.772(5)	0.639(1)	-0.00334(8)	0.000014(2)			
1171.140276(6)	8	4	E	8	5	E	^p Q(8,5,E)	29.90(4)	0.0593(1)	0.0590	0.774(5)	0.659(3)	-0.00279(12)	0.000020(2)	0.0820(3)		
1171.170415(11)	12	5	A1	12	6	A2	^p Q(12,6,A2)	21.32(5)	0.0512(2)	0.0539	0.754(16)	0.611(1)	-0.00337(14)		0.0721(10)		
1171.352383(5)	2	1	A1	1	0	A2	^R R(1,0,A2)	52.75(2)	0.0659(0)	0.0709	0.843(1)	0.763(6)	-0.00072(5)	0.000004(1)	0.0903(1)		
1171.893414(6)	7	4	E	7	5	E	^p Q(7,5,E)	30.81(2)	0.0614(1)	0.0614	0.822(3)	0.687(5)	-0.00197(8)	0.000012(1)	0.0847(2)		
1172.232987(7)	11	5	A1	11	6	A2	^p Q(11,6,A2)	28.2(3)	0.0524(1)	0.0549	0.720(7)	0.619(1)	-0.00364(7)	0.000020(2)			
1172.570194(6)	6	4	E	6	5	E	^p Q(6,5,E)	27.99(5)	0.0655(2)	0.0640	0.858(7)	0.718(6)	-0.00196(15)	0.000020(2)	0.0870(3)		
1172.601008(5)	3	3	E	2	2	E	^R R(2,2,E)	77.51(4)	0.0653(1)	0.0663	0.851(1)	0.744(6)	-0.00111(6)	0.000004(2)	0.0874(1)		
1173.163727(6)	5	4	E	5	5	E	^p Q(5,5,E)	18.56(3)	0.0695(2)	0.0657	0.854(3)	0.742(7)			0.0907(3)		
1173.240002(6)	10	5	A1	10	6	A2	^p Q(10,6,A2)	35.79(4)	0.0544(1)	0.0563	0.750(5)	0.633(1)	-0.00318(7)	0.000016(1)	0.0768(3)		
1173.771460(25)	13	6	E	13	7	E	^p Q(13,7,E)	6.35(2)	0.0500(3)	0.0532	0.647(37)	0.605(1)	-0.00477(31)		0.0601(32)		
1174.183837(6)	9	5	A1	9	6	A2	^p Q(9,6,A2)	42.51(3)	0.0570(1)	0.0584	0.754(4)	0.655(2)	-0.00303(6)	0.000014(1)			
1174.973264(42)	12	6	E	12	7	E	^p Q(12,7,E)	8.89(3)	0.0505(4)	0.0543	0.587(35)	0.614(1)	-0.00560(45)	0.000068(8)	0.0594(32)		
1174.978732(18)	2	0	E	1	1	E	^R R(1,1,E)	7.98(2)	0.0671(5)	0.0710	0.843(7)	0.764(6)		0.0952(9)			
1175.743244(6)	3	2	E	2	1	E	^R R(2,1,E)	57.05(2)	0.0634(1)	0.0679	0.836(1)	0.743(6)	-0.00086(5)	0.000009(2)	0.0835(8)	0.784(23)	
1175.852436(6)	7	5	A1	7	6	A2	^p Q(7,6,A2)	42.70(3)	0.0638(1)	0.0633	0.817(3)	0.712(6)	-0.00102(6)		0.0852(2)		
1176.115511(13)	11	6	E	11	7	E	^p Q(11,7,E)	11.51(2)	0.0514(2)	0.0559	0.744(17)	0.629(1)	-0.00429(16)		0.0748(16)		
1176.563597(6)	6	5	A1	6	6	A2	^p Q(6,6,A2)	28.76(2)	0.0666(1)	0.0647	0.858(3)	0.735(7)			0.0893(3)		
1176.974032(5)	4	4	A1	3	3	A2	^R R(3,3,A2)	186.38(3)	0.0630(0)	0.0647	0.822(1)	0.734(6)	-0.00108(3)	0.000004(2)	0.0814(4)	0.801(11)	
1177.191505(10)	10	6	E	10	7	E	^p Q(10,7,E)	14.55(2)	0.0556(2)	0.0580	0.692(12)	0.650(2)	-0.00307(14)		0.0768(10)		
1178.194155(9)	9	6	E	9	7	E	^p Q(9,7,E)	16.24(2)	0.0598(2)	0.0603	0.742(9)	0.677(3)	-0.00225(13)		0.0798(7)		
1178.629294(6)	3	1	A2	2	0	A1	^R R(2,0,A1)	67.23(2)	0.0667(0)	0.0695	0.845(1)	0.748(6)	-0.00159(4)	0.000010(2)	0.0889(2)		
1178.921575(23)	12	7	E	12	8	E	^p Q(12,8,E)	7.19(2)	0.0498(3)	0.0556		0.624(1)	-0.00413(22)		0.0683(28)		
1179.116925(8)	8	6	E	8	7	E	^p Q(8,7,E)	15.21(2)	0.0608(2)	0.0626	0.801(8)	0.705(5)			0.0878(7)		
1179.953709(9)	7	6	E	7	7	E	^p Q(7,7,E)	11.28(3)	0.0648(3)	0.0638	0.858(9)	0.728(6)		0.000047(7)	0.0759(9)		

1179.987401(6)	4	3	E	3	2	E	^p R(3,2,E)	76.03(3)	0.0651(1)	0.0663	0.846(1)	0.733(6)	-0.00093(5)	0.000013(1)	0.0860(2)	0.750(0)
1180.144243(23)	11	7	E	11	8	E	^p Q(11,8,E)	9.31(4)	0.0497(2)	0.0576	0.757(23)	0.644(1)	-0.00239(20)			
1181.390665(5)	5	5	E	4	4	E	^p R(4,4,E)	97.66(2)	0.0587(0)	0.0632	0.801(1)	0.723(6)	-0.00126(3)	0.000007(2)	0.0763(5)	0.843(16)
1182.350649(11)	9	7	E	9	8	E	^p Q(9,8,E)	10.25(3)	0.0590(2)	0.0619		0.695(4)			0.0631(13)	
1182.476326(7)	3	0	E	2	1	E	^p R(2,1,E)	14.04(2)	0.0677(2)	0.0695	0.854(3)	0.749(6)			0.0906(3)	
1183.014330(15)	12	8	A1	12	9	A2	^p Q(12,9,A2)	11.22(2)	0.0511(2)	0.0572		0.637(1)	-0.00246(15)		0.0670(19)	
1183.099278(6)	4	2	E	3	1	E	^p R(3,1,E)	61.95(2)	0.0635(0)	0.0666	0.835(1)	0.725(6)	-0.00065(5)	0.000008(1)	0.0820(2)	0.840(16)
1183.323054(12)	8	7	E	8	8	E	^p Q(8,8,E)	7.71(1)	0.0645(3)	0.0628	0.879(16)	0.718(6)	0.00416(23)		0.0833(14)	
1184.273226(5)	5	4	A1	4	3	A2	^p R(4,3,A2)	170.58(3)	0.0648(0)	0.0653	0.836(1)	0.727(6)	-0.00102(3)	0.000008(2)	0.0826(3)	0.846(9)
1184.320459(12)	11	8	A1	11	9	A2	^p Q(11,9,A2)	13.97(3)	0.0544(2)	0.0592		0.659(2)			0.0681(15)	
1185.536801(10)	10	8	A1	10	9	A2	^p Q(10,9,A2)	13.87(2)	0.0583(2)	0.0611		0.684(4)			0.0787(12)	
1185.744718(6)	4	1	A1	3	0	A2	^p R(3,0,A2)	76.92(3)	0.0668(0)	0.0679	0.847(1)	0.734(6)	-0.00111(4)	0.000006(1)	0.0883(2)	
1185.851958(5)	6	6	E	5	5	E	^p R(5,5,E)	92.39(3)	0.0542(0)	0.0620	0.751(1)	0.712(5)	-0.00157(3)	0.000006(2)	0.0745(1)	
1185.990482(10)	3	1	E	2	2	E	^p R(2,2,E)	5.17(1)	0.0704(4)	0.0691	0.871(10)	0.753(7)	-0.00427(40)		0.0906(9)	
1186.658408(11)	9	8	A1	9	9	A2	^p Q(9,9,A2)	10.61(2)	0.0632(2)	0.0618		0.707(5)	0.00507(17)		0.0786(12)	
1187.263042(11)	5	3	E	4	2	E	^p R(4,2,E)	73.60(2)	0.0634(1)	0.0644	0.843(1)	0.706(6)	-0.00091(6)	0.000009(1)	0.0806(2)	
1188.602255(5)	6	5	E	5	4	E	^p R(5,4,E)	85.56(2)	0.0635(0)	0.0645	0.816(1)	0.721(6)	-0.00158(4)	0.000006(2)	0.0827(2)	
1189.904653(6)	4	0	E	3	1	E	^p R(3,1,E)	16.88(1)	0.0670(1)	0.0679	0.843(2)	0.736(6)	-0.00180(14)		0.0898(3)	
1190.322385(7)	5	2	E	4	1	E	^p R(4,1,E)	65.66(5)	0.0631(1)	0.0651	0.832(1)	0.711(6)	-0.00080(7)	0.000009(1)	0.0848(16)	0.718(42)
1190.358540(6)	7	7	A1	6	6	A2	^p R(6,6,A2)	162.96(8)	0.0507(1)	0.0607	0.706(1)	0.699(4)	-0.00141(3)	0.000008(2)	0.0689(4)	0.693(13)
1191.463969(5)	6	4	A1	5	3	A2	^p R(5,3,A2)	154.91(3)	0.0635(0)	0.0630	0.826(1)	0.697(5)	-0.00108(3)	0.000009(2)	0.0901(4)	0.581(11)
1192.699138(6)	5	1	A2	4	0	A1	^p R(4,0,A1)	81.58(2)	0.0660(0)	0.0663	0.847(1)	0.722(6)	-0.00113(4)	0.000009(2)	0.0881(1)	
1192.976955(6)	7	6	E	6	5	E	^p R(6,5,E)	77.01(3)	0.0606(0)	0.0636	0.793(1)	0.713(6)	-0.00160(4)	0.000012(2)	0.0815(2)	
1193.384516(7)	4	1	E	3	2	E	^p R(3,2,E)	9.66(1)	0.0664(2)	0.0670	0.854(3)	0.733(6)			0.0896(5)	
1194.417528(6)	6	3	E	5	2	E	^p R(5,2,E)	69.73(2)	0.0622(0)	0.0626	0.818(1)	0.685(5)	-0.00076(4)	0.000007(2)	0.0821(1)	
1194.910923(5)	8	8	E	7	7	E	^p R(7,7,E)	65.71(2)	0.0444(0)	0.0596	0.646(2)	0.685(3)	-0.00146(3)	0.000008(2)	0.0630(1)	
1195.706526(6)	7	5	E	6	4	E	^p R(6,4,E)	72.99(3)	0.0624(0)	0.0622	0.810(1)	0.692(5)	-0.00154(4)	0.000010(2)	0.0818(2)	
1197.278810(7)	5	0	E	4	1	E	^p R(4,1,E)	17.21(2)	0.0667(1)	0.0663	0.828(2)	0.722(6)			0.0896(3)	
1197.396019(22)	6	2	E	5	1	E	^p R(5,1,E)	66.96(8)	0.0699(3)	0.0637	0.761(4)	0.700(6)		0.000013(2)	0.0799(23)	
1197.396721(18)	8	7	A1	7	6	A2	^p R(7,6,A2)	129.39(10)	0.0556(1)	0.0627	0.751(3)	0.703(5)	-0.00224(14)	0.000007(1)	0.0800(18)	
1198.536940(9)	7	4	A2	6	3	A1	^p R(6,3,A1)	67.72(1)	0.0618(0)	0.0607	0.797(1)	0.668(4)	-0.00121(2)		0.0746(1)	0.948(2)
1198.542387(15)	7	4	A1	6	3	A2	^p R(6,3,A2)	67.72(1)	0.0618(0)	0.0607	0.797(1)	0.668(4)	-0.00121(2)		0.0746(1)	0.948(2)
1199.493392(8)	6	1	A1	5	0	A2	^p R(5,0,A2)	80.71(4)	0.0665(1)	0.0647	0.818(2)	0.711(6)	-0.00120(7)		0.0841(2)	
1199.509368(8)	9	9	E	8	8	E	^p R(8,8,E)	49.69(7)	0.0394(1)	0.0585	0.585(5)	0.669(2)	-0.00206(7)	0.000011(1)		
1199.994381(6)	8	6	E	7	5	E	^p R(7,5,E)	62.68(3)	0.0599(1)	0.0616	0.797(2)	0.688(5)	-0.00175(5)	0.000011(1)	0.0822(2)	
1200.701589(7)	5	1	E	4	2	E	^p R(4,2,E)	12.71(1)	0.0656(2)	0.0654	0.839(4)	0.716(6)			0.000016(2)	
1201.439678(6)	7	3	E	6	2	E	^p R(6,2,E)	63.68(2)	0.0609(1)	0.0611	0.803(1)	0.672(4)	-0.00090(4)	0.000004(1)	0.0814(2)	
1201.862535(6)	9	8	E	8	7	E	^p R(8,7,E)	50.14(3)	0.0544(1)	0.0618	0.749(3)	0.691(4)	-0.00180(5)	0.000018(1)		
1202.695902(6)	8	5	E	7	4	E	^p R(7,4,E)	60.73(3)	0.0602(1)	0.0597	0.799(2)	0.661(3)	-0.00111(5)	0.000010(1)	0.0799(2)	
1204.304894(16)	7	2	E	6	1	E	^p R(6,1,E)	63.93(11)	0.0640(1)	0.0624	0.871(3)	0.690(5)	-0.00143(11)	0.000015(1)	0.0837(4)	
1204.327733(7)	9	7	A1	8	6	A2	^p R(8,6,A2)	100.34(10)	0.0579(1)	0.0610	0.777(3)	0.680(3)	-0.00212(6)	0.000026(1)	0.0791(2)	
1204.614848(7)	6	0	E	5	1	E	^p R(5,1,E)	15.14(2)	0.0662(2)	0.0647	0.822(4)	0.711(6)	-0.00149(11)		0.0877(4)	
1205.485111(8)	8	4	A1	7	3	A2	^p R(7,3,A2)	57.72(3)	0.0655(1)	0.0590	0.794(2)	0.649(3)	-0.00140(3)		0.0854(1)	
1205.529251(8)	8	4	A2	7	3	A1	^p R(7,3,A1)	48.93(4)	0.0655(1)	0.0590	0.794(2)	0.649(3)	-0.00140(3)		0.0854(1)	
1206.128962(6)	7	1	A2	6	0	A1	^p R(6,0,A1)	75.67(2)	0.0653(0)	0.0633	0.829(1)	0.700(6)	-0.00191(4)	0.000009(1)	0.0845(2)	
1206.374111(7)	10	9	E	9	8	E	^p R(9,8,E)	36.01(4)	0.0508(1)	0.0609	0.706(5)	0.675(3)	-0.00266(8)	0.000010(1)	0.0746(3)	
1206.898332(6)	9	6	E	8	5	E	^p R(8,5,E)	49.45(3)	0.0578(1)	0.0591	0.778(2)	0.658(2)	-0.00190(5)	0.000009(1)		
1207.951494(7)	6	1	E	5	2	E	^p R(5,2,E)	13.50(2)	0.0636(2)	0.0639	0.830(4)	0.703(6)	-0.00221(16)	0.000021(2)		
1208.318059(6)	8	3	E	7	2	E	^p R(7,2,E)	56.01(2)	0.0599(1)	0.0599	0.796(2)	0.664(4)	-0.00111(5)			
1208.706761(6)	10	8	E	9	7	E	^p R(9,7,E)	37.57(3)	0.0557(1)	0.0604	0.744(4)	0.669(2)	-0.00141(6)	0.000015(1)	0.0766(3)	
1208.844713(8)	11	11	E	10	10	E	^p R(10,10,E)	23.03(2)	0.0306(1)	0.0564	0.445(7)	0.639(1)	-0.00237(5)	0.000012(1)		
1209.563871(6)	9	5	E	8	4	E	^p R(8,4,E)	48.62(3)	0.0580(1)	0.0576	0.773(2)	0.638(1)	-0.00125(5)			
1210.931527(6)	11	10	A1	10	9	A2	^p R(10,9,A2)	49.31(4)	0.0479(1)	0.0599	0.677(5)	0.659(1)	-0.00241(5)	0.000019(1)	0.0704(3)	
1211.037407(6)	8	2	E	7	1	E	^p R(7,1,E)	58.58(4)	0.0631(1)	0.0612	0.817(2)	0.681(5)	-0.00140(6)	0.000008(1)	0.0828(2)	

Table 5 (continued)

Position, cm ⁻¹	J	K'	S'	J''	K''	S''	Assignment	Int*10 ^{25a}	$b_L^0(N_2)$ expt, ^b	$b_L^0(N_2)$ calc. ^b	n_1 expt	n_1 calc.	$\delta^0(N_2)$ expt ^b	$\delta'(N_2)$ expt ^c	$b_L^0(self)$ expt ^b	n_2 expt
1211.145943(6)	10	7	A1	9	6	A2	^p R(9,6,A2)	75.55(4)	0.0559(1)	0.0586	0.747(2)	0.653(2)	-0.00200(4)	0.000012(1)	0.0781(2)	
1211.492823(9)	6	2	A1	5	3	A2	^p R(5,3,A2)	8.88(1)	0.0635(1)	0.0632	0.843(1)	0.697(6)	-0.00185(9)	0.000018(1)	0.0953(4)	
1211.517931(9)	6	2	A2	5	3	A1	^p R(5,3,A1)	8.96(1)	0.0635(1)	0.0632	0.843(1)	0.697(6)	-0.00185(9)	0.000018(1)	0.0953(4)	
1211.927987(8)	7	0	E	6	1	E	^p R(6,1,E)	11.90(2)	0.0652(3)	0.0633	0.822(5)	0.700(6)				0.0892(6)
1212.252462(6)	9	4	A1	8	3	A2	^p R(8,3,A2)	46.20(3)	0.0642(1)	0.0577	0.809(2)	0.639(2)	-0.00123(3)	0.000003(2)	0.0853(1)	
1212.298834(8)	9	4	A2	8	3	A1	^p R(8,3,A1)	47.57(4)	0.0642(1)	0.0577	0.809(2)	0.639(2)	-0.00123(3)	0.000003(2)	0.0853(1)	
1212.607277(6)	8	1	A1	7	0	A2	^p R(7,0,A2)	66.81(3)	0.0644(1)	0.0620	0.824(1)	0.690(5)	-0.00221(5)	0.000018(1)	0.0852(2)	
1213.131507(8)	11	9	E	10	8	E	^p R(10,8,E)	25.65(3)	0.0519(1)	0.0596	0.708(7)	0.656(1)	-0.00251(9)			0.0814(6)
1213.581159(12)	12	12	E	11	11	E	^p R(11,11,E)	14.96(2)	0.0277(1)	0.0554	0.36(14)	0.627(1)	-0.00187(8)	0.000021(2)	0.0434(12)	
1213.682846(7)	10	6	E	9	5	E	^p R(9,5,E)	37.66(5)	0.0562(1)	0.0568	0.721(6)	0.633(1)	-0.00148(14)			0.0778(3)
1215.042024(6)	9	3	E	8	2	E	^p R(8,2,E)	47.34(3)	0.0597(1)	0.0589	0.783(2)	0.656(3)	-0.00134(6)	0.000006(1)	0.0806(2)	
1215.145227(8)	7	1	E	6	2	E	^p R(6,2,E)	12.92(2)	0.0637(2)	0.0625	0.811(5)	0.692(5)	-0.0033(21)			0.0863(5)
1215.208733(12)	6	3	E	5	4	E	^p R(5,4,E)	4.75(1)	0.0679(5)	0.0643	0.893(11)	0.719(7)				0.0916(14)
1215.438903(7)	11	8	E	10	7	E	^p R(10,7,E)	26.76(3)	0.0529(1)	0.0582	0.728(7)	0.645(1)	-0.00195(9)			0.0777(5)
1215.534491(11)	12	11	E	11	10	E	^p R(11,10,E)	16.08(3)	0.0451(2)	0.0588	0.627(14)	0.644(1)	-0.00389(12)	0.000027(3)	0.0722(13)	
1216.303890(6)	10	5	E	9	4	E	^p R(9,4,E)	37.61(3)	0.0561(1)	0.0561	0.765(4)	0.624(1)	-0.00146(7)			0.0771(3)
1217.588040(11)	9	2	E	8	1	E	^p R(8,1,E)	50.40(5)	0.0626(1)	0.0602	0.803(4)	0.671(3)		0.000015(2)	0.0831(4)	
1217.601718(14)	12	10	A1	11	9	A2	^p R(11,9,A2)	33.76(7)	0.0499(2)	0.0588	0.669(13)	0.643(1)	-0.00339(17)	0.000021(3)	0.077(12)	
1217.846109(6)	11	7	A1	10	6	A2	^p R(10,6,A2)	55.02(3)	0.0532(1)	0.0564	0.728(3)	0.629(1)	-0.00208(5)	0.000011(1)	0.0765(2)	
1218.362994(12)	13	13	A1	12	12	A2	^p R(12,12,A2)	17.17(2)	0.0239(1)	0.0545	0.264(14)	0.616(1)	-0.00236(6)	0.000016(1)	0.0481(15)	
1218.616479(8)	7	2	A2	6	3	A1	^p R(6,3,A1)	9.94(1)	0.0674(2)	0.0615	0.872(5)	0.679(5)	-0.00206(7)	0.000012(1)	0.0889(3)	
1218.661262(9)	7	2	A1	6	3	A2	^p R(6,3,A2)	9.91(2)	0.0674(2)	0.0615	0.872(5)	0.679(5)	-0.00206(7)	0.000012(1)	0.0889(3)	
1218.930369(9)	9	1	A2	8	0	A1	^p R(8,0,A1)	55.98(11)	0.0620(1)	0.0608	0.797(3)	0.678(4)				0.0843(5)
1218.933810(9)	10	4	A2	9	3	A1	^p R(9,3,A1)	37.28(4)	0.0641(0)	0.0568	0.809(0)	0.633(1)	-0.00201(4)			0.0865(3)
1218.969303(6)	10	4	A1	9	3	A2	^p R(9,3,A2)	37.28(4)	0.0641(0)	0.0568	0.809(0)	0.633(1)	-0.00201(4)			0.0865(3)
1219.229417(9)	8	0	E	7	1	E	^p R(7,1,E)	8.64(2)	0.0640(3)	0.0620	0.850(8)	0.690(5)		0.000034(4)	0.0857(9)	
1219.777253(10)	12	9	E	11	8	E	^p R(11,8,E)	17.98(3)	0.0507(2)	0.0577	0.677(11)	0.635(1)	-0.00148(12)	0.000018(2)	0.0806(11)	
1220.342003(7)	11	6	E	10	5	E	^p R(10,5,E)	27.91(3)	0.0541(1)	0.0551	0.735(6)	0.616(1)	-0.00117(8)	0.000011(2)	0.0768(4)	
1221.602529(6)	10	3	E	9	2	E	^p R(9,2,E)	38.94(3)	0.0601(1)	0.0581	0.769(3)	0.648(2)	-0.00172(6)	0.000007(1)	0.0757(3)	
1222.054179(9)	12	8	E	11	7	E	^p R(11,7,E)	18.98(3)	0.0509(1)	0.0561	0.694(10)	0.623(1)	-0.00125(10)	0.000018(2)	0.0708(9)	
1222.911308(7)	11	5	E	10	4	E	^p R(10,4,E)	27.98(3)	0.0546(1)	0.0551	0.777(5)	0.616(1)	-0.00124(7)			0.0752(4)
1223.189452(68)	14	14	E	13	13	E	^p R(13,13,E)	4.61(5)	0.0209(3)	0.0537	0.580(53)	0.608(1)	-0.00397(19)			0.0537(10)
1223.955802(6)	10	2	E	9	1	E	^p R(9,1,E)	41.50(3)	0.0621(1)	0.0592	0.811(3)	0.660(2)	-0.00188(6)	0.000010(1)	0.0795(3)	
1224.160571(10)	13	10	A1	12	9	A2	^p R(12,9,A2)	22.36(3)	0.0479(1)	0.0571	0.653(11)	0.625(1)	-0.00276(8)			0.0723(22)
1224.423081(7)	12	7	A1	11	6	A2	^p R(11,6,A2)	38.64(3)	0.0512(1)	0.0546	0.728(5)	0.612(1)	-0.00221(5)	0.000009(1)	0.0713(4)	
1225.100230(6)	10	1	A1	9	0	A2	^p R(9,0,A2)	45.07(3)	0.0633(1)	0.0598	0.803(3)	0.665(3)	-0.00134(6)	0.000008(1)	0.0785(9)	0.819(27)
1225.452547(7)	11	4	A1	10	3	A2	^p R(10,3,A2)	28.71(3)	0.0620(1)	0.0561	0.752(6)	0.627(1)	-0.00227(4)	0.000016(1)	0.0825(2)	
1225.488360(7)	11	4	A2	10	3	A1	^p R(10,3,A1)	28.59(3)	0.0620(1)	0.0561	0.752(6)	0.627(1)	-0.00227(4)	0.000016(1)	0.0825(2)	
1225.671923(9)	8	2	A1	7	3	A2	^p R(7,3,A2)	9.24(1)	0.0656(1)	0.0601	0.829(5)	0.668(4)	-0.00318(7)	0.000018(1)	0.0891(4)	
1225.745502(9)	8	2	A2	7	3	A1	^p R(7,3,A1)	9.14(2)	0.0656(1)	0.0601	0.829(5)	0.668(4)	-0.00318(7)	0.000018(1)	0.0891(4)	
1226.100182(17)	7	4	E	6	5	E	^p R(6,5,E)	3.15(1)	0.0666(6)	0.0636	0.868(19)	0.718(7)				0.0868(20)
1226.307017(14)	13	9	E	12	8	E	^p R(12,8,E)	11.90(2)	0.0484(2)	0.0558	0.674(18)	0.617(1)	-0.00196(13)			0.0673(19)
1226.525196(13)	9	0	E	8	1	E	^p R(8,1,E)	5.71(1)	0.0628(4)	0.0609	0.831(14)	0.679(4)				0.0815(15)
1226.870391(9)	12	6	E	11	5	E	^p R(11,5,E)	20.02(3)	0.0530(1)	0.0540	0.761(9)	0.607(1)	-0.00181(9)			0.0740(8)
1227.993000(7)	11	3	E	10	2	E	^p R(10,2,E)	29.66(3)	0.0584(1)	0.0573	0.796(5)	0.639(1)	-0.00161(9)			0.0805(4)
1228.547887(14)	13	8	E	12	7	E	^p R(12,7,E)	12.65(2)	0.0478(2)	0.0543	0.727(20)	0.607(1)	-0.00209(17)			0.0748(18)
1229.311759(11)	8	3	E	7	4	E	^p R(7,4,E)	6.71(1)	0.0605(3)	0.0596	0.845(12)	0.662(4)	-0.00391(36)			0.0859(12)
1229.389521(10)	12	5	E	11	4	E	^p R(11,4,E)	19.74(3)	0.0544(2)	0.0544	0.736(17)	0.611(1)				0.0788(11)
1229.409797(11)	9	1	E	8	2	E	^p R(8,2,E)	8.56(2)	0.0624(5)	0.0602	0.837(16)	0.672(4)				0.0827(14)

1230.143728(7)	11	2	E	10	1	E	^R R(10,1,E)	31.50(3)	0.0603(1)	0.0582	0.786(5)	0.648(1)	-0.00224(9)	0.000021(2)	0.0836(4)
1230.604297(15)	14	10	A1	13	9	A2	^R R(13,9,A2)	14.64(3)	0.0464(2)	0.0554		0.609(1)			
1230.871883(9)	13	7	A1	12	6	A2	^R R(12,6,A2)	26.33(3)	0.0502(1)	0.0534	0.634(10)	0.601(2)	-0.00228(9)	0.000025(2)	
1231.119627(7)	11	1	A2	10	0	A1	^R R(10,0,A1)	34.11(3)	0.0621(1)	0.0587	0.789(5)	0.652(1)	-0.00162(8)	0.000021(2)	0.0841(4)
1231.811182(9)	12	4	A2	11	3	A1	^R R(11,3,A1)	20.94(3)	0.0606(1)	0.0555	0.813(9)	0.621(1)	-0.00142(5)	0.000021(1)	0.0850(3)
1231.848733(9)	12	4	A1	11	3	A2	^R R(11,3,A2)	20.92(3)	0.0606(1)	0.0555	0.813(9)	0.621(1)	-0.00142(5)	0.000021(1)	0.0850(3)
1232.667550(11)	9	2	A2	8	3	A1	^P R(8,3,A1)	7.95(1)	0.0626(2)	0.0591	0.841(5)	0.659(3)	-0.00227(12)	0.000023(3)	0.0882(9)
1232.781012(11)	9	2	A1	8	3	A2	^P R(8,3,A2)	7.98(1)	0.0626(2)	0.0591	0.841(5)	0.659(3)	-0.00227(12)	0.000023(3)	0.0882(9)
1233.060408(72)	15	12	E	14	11	E	^R R(14,11,E)	3.80(3)	0.0431(5)	0.0559		0.606(1)	-0.00415(36)		
1233.263806(13)	13	6	E	12	5	E	^R R(12,5,E)	13.92(2)	0.0528(2)	0.0533	0.652(18)	0.601(2)	-0.00184(16)		
1234.209695(8)	12	3	E	11	2	E	^R R(11,2,E)	21.97(3)	0.0580(1)	0.0565	0.747(8)	0.630(1)	-0.00224(11)		0.0810(7)
1234.915629(22)	14	8	E	13	7	E	^R R(13,7,E)	8.20(2)	0.0466(3)	0.0530	0.579(31)	0.597(2)			0.0637(30)
1235.820952(15)	13	5	E	12	4	E	^R R(12,4,E)	10.34(2)	0.0568(3)	0.0539	0.717(21)	0.607(1)	-0.00145(11)		0.0776(19)
1236.157291(8)	12	2	E	11	1	E	^R R(11,1,E)	23.41(4)	0.0598(2)	0.0574	0.753(10)	0.636(1)	-0.00228(12)	0.000024(3)	0.0849(7)
1236.257241(13)	9	3	E	8	4	E	^P R(8,4,E)	6.25(1)	0.0598(4)	0.0581	0.795(16)	0.647(2)	-0.00328(20)	0.000054(6)	0.0815(15)
1236.501073(15)	10	1	E	9	2	E	^P R(9,2,E)	6.03(1)	0.0621(4)	0.0592	0.798(19)	0.661(2)			0.0839(17)
1236.960540(17)	8	5	A1	7	6	A2	^P R(7,6,A2)	4.13(1)	0.0672(7)	0.0631		0.716(6)			0.0858(20)
1236.991242(8)	12	1	A1	11	0	A2	^P R(11,0,A2)	24.53(4)	0.0608(2)	0.0578	0.801(11)	0.640(1)	-0.00197(14)		0.0879(7)
1237.188272(13)	14	7	A1	13	6	A2	^R R(13,6,A2)	17.18(3)	0.0494(2)	0.0525	0.710(16)	0.595(2)	-0.00223(12)		0.0724(16)
1238.006728(12)	13	4	A1	12	3	A2	^R R(12,3,A2)	14.92(2)	0.0599(2)	0.0549	0.803(16)	0.614(1)	-0.00191(6)	0.000015(1)	0.0869(6)
1238.044758(12)	13	4	A2	12	3	A1	^R R(12,3,A1)	14.76(2)	0.0599(2)	0.0549	0.803(16)	0.614(1)	-0.00191(6)	0.000015(1)	0.0869(6)
1239.611629(14)	10	2	A1	9	3	A2	^P R(9,3,A2)	6.24(1)	0.0641(5)	0.0582	0.660(24)	0.650(2)			0.0858(18)
1239.778257(20)	10	2	A2	9	3	A1	^P R(9,3,A1)	6.37(2)	0.0636(8)	0.0582	0.883(35)	0.650(2)		0.000111(13)	0.0873(27)
1239.952806(17)	9	4	E	8	5	E	^P R(8,5,E)	4.29(1)	0.0595(5)	0.0584	0.769(23)	0.655(3)		0.000074(8)	0.0755(20)
1240.251762(11)	13	3	E	12	2	E	^R R(12,2,E)	15.56(2)	0.0576(2)	0.0558	0.682(14)	0.621(1)	-0.00192(13)		0.0804(13)
1241.698227(19)	14	5	E	13	4	E	^R R(13,4,E)	8.62(2)	0.0541(2)	0.0535		0.602(2)	-0.00111(9)	0.000020(2)	
1242.002920(10)	13	2	E	12	1	E	^R R(12,1,E)	16.84(2)	0.0604(1)	0.0565		0.626(1)	-0.00231(12)		
1242.717923(10)	13	1	A2	12	0	A1	^R R(12,0,A1)	17.32(3)	0.0608(2)	0.0569		0.628(1)	-0.00238(12)		0.0810(11)
1243.142558(16)	10	3	E	9	4	E	^P R(9,4,E)	5.28(1)	0.0609(3)	0.0570		0.638(1)	-0.00328(31)		
1243.369265(19)	15	7	A2	14	6	A1	^R R(14,6,A1)	10.97(2)	0.0493(2)	0.0520		0.591(4)	-0.00199(15)		
1244.037172(17)	14	4	A2	13	3	A1	^R R(13,3,A1)	9.97(2)	0.0614(2)	0.0544	0.690(10)	0.608(1)	-0.00219(8)	0.000017(2)	0.0733(10)
1244.072667(17)	14	4	A1	13	3	A2	^R R(13,3,A2)	9.82(2)	0.0614(2)	0.0544	0.690(10)	0.608(1)	-0.00219(8)	0.000017(2)	0.0733(10)
1246.120908(16)	14	3	E	13	2	E	^R R(13,2,E)	10.71(2)	0.0578(2)	0.0552		0.612(1)	-0.00228(17)	0.000020(2)	0.0744(21)
1246.511979(20)	11	2	A2	10	3	A1	^P R(10,3,A1)	4.50(1)	0.0667(4)	0.0574		0.641(1)	-0.00363(14)	0.000020(2)	
1246.746775(21)	11	2	A1	10	3	A2	^P R(10,3,A2)	4.43(1)	0.0667(4)	0.0574		0.641(1)	-0.00363(14)	0.000020(2)	
1246.767860(20)	10	4	E	9	5	E	^P R(9,5,E)	3.99(1)	0.0570(4)	0.0567		0.635(1)	-0.00723(45)		
1248.302906(14)	14	1	A1	13	0	A2	^P R(13,0,A2)	11.48(2)	0.0600(2)	0.0560	0.673(20)	0.618(1)	-0.00183(15)		
1249.414534(28)	16	7	A1	15	6	A2	^R R(15,6,A2)	3.47(1)	0.0517(3)	0.0516		0.587(5)			
1249.414534(28)	16	7	A2	15	6	A1	^R R(15,6,A1)	3.47(1)	0.0517(3)	0.0516		0.587(5)			
1250.54476(15)	10	5	A1	9	6	A2	^P R(9,6,A2)	5.53(1)	0.0581(3)	0.0578		0.652(2)		0.000020(2)	
1251.820632(38)	15	3	E	14	2	E	^P R(14,2,E)	7.02(3)	0.0562(3)	0.0545		0.604(2)	-0.00321(26)	0.000020(2)	
1253.518248(26)	11	4	E	10	5	E	^P R(10,5,E)	3.30(1)	0.0550(5)	0.0555		0.623(1)			
1253.694913(31)	12	2	A2	11	3	A1	^P R(11,3,A1)	3.06(1)	0.0619(6)	0.0566		0.633(3)		0.000020(2)	
1253.749377(23)	15	1	A2	14	0	A1	^R R(14,0,A1)	7.43(2)	0.0597(3)	0.0552		0.609(1)			

^a cm/molecule.^b cm⁻¹ atm⁻¹.^c cm⁻¹ atm⁻¹ K⁻¹.

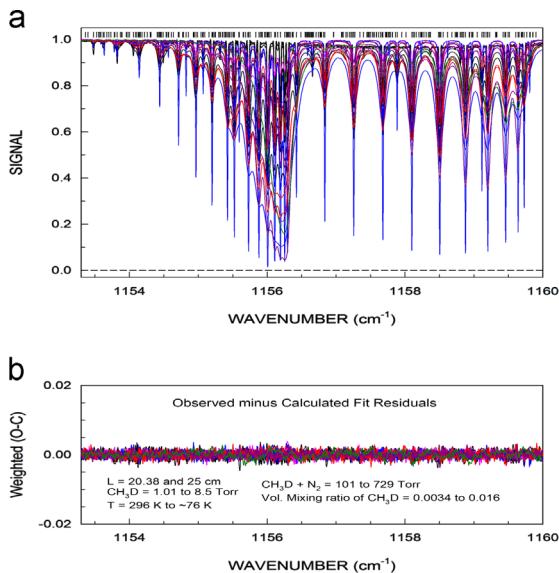


Fig. 4. An example of a multispectrum fit of $^{12}\text{CH}_3\text{D}$ Triad near 1156 cm^{-1} . 20 spectra are included in this fit. This spectral region shows transitions from the $^R\text{Q}(J'', K''=0)$ series (band head near 1156.3 cm^{-1}) and transitions from the $^P\text{Q}(J'', K''=1)$ series (high-wavenumber side), both from the ν_6 band. The observed spectra are plotted in the upper panel (a) and the weighted observed minus calculated differences are shown in the lower panel (b). The horizontal dash line at the bottom of panel (a) represents the 100% absorption level. The short vertical lines seen at the top of the absorption features in (a) correspond to positions of transitions included in the fit. Color codes: room-temperature spectra with the 25 cm cell (black); room-temperature spectra with the 20.38 cm cell (pink); spectra at 240 K (red); spectra at 189 K (blue); spectra at ~ 135 K (dark pink); spectra at ~ 76 K (dark green). (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

preliminary tests, we retained the dominant contributions with $l_1 \leq 3$ and $l_2 \leq 2$: $V_{123}^{00 \text{ eda}}$, $V_{101}^{00 \text{ da}}$, $V_{121}^{00 \text{ da}}$, $V_{224}^{00 \text{ ia}}$, $V_{202}^{00 \text{ ia}}$, $V_{303}^{00 \text{ ea}}$, $V_{323}^{00 \text{ ea}}$, and $V_{325}^{00 \text{ ea}}$. The molecular parameters for the accounted long-range and atom–atom interactions are gathered in Tables 3 and 4, respectively.

To get the isotropic potential governing the relative-motion trajectories we fitted the $V_{000}^0(r)$ curve by a standard 12:6 Lennard–Jones function and slightly optimized the σ -parameter (defined below) value to improve the agreement with measurements for high J values (a procedure of “trials” similar to that previously employed for the $\text{CH}_3\text{Cl}-\text{H}_2$ system [66]). The Lennard–Jones parameters obtained are $\varepsilon=83.50 \text{ K}$ and $\sigma=3.838 \text{\AA}$. The molecular rotational constants used in the calculations are $A_0=5.2502 \text{ cm}^{-1}$, $B_0=3.8800 \text{ cm}^{-1}$ [67] for the ground state of the active molecule and $A=5.28744 \text{ cm}^{-1}$, $B=3.87553 \text{ cm}^{-1}$ [28] for the vibrationally excited ν_6 state whereas $B_0=1.989622 \text{ cm}^{-1}$ [68] for the linear perturbing molecule. At the temperatures of interest only the vibrational ground state has significant rotational populations.

5. Spectroscopic results and comparisons with theoretical results

In Fig. 2 we have plotted examples of pure-gas (panel (a)) and lean $\text{CH}_3\text{D}-\text{N}_2$ -mixture (panel (b)) spectra

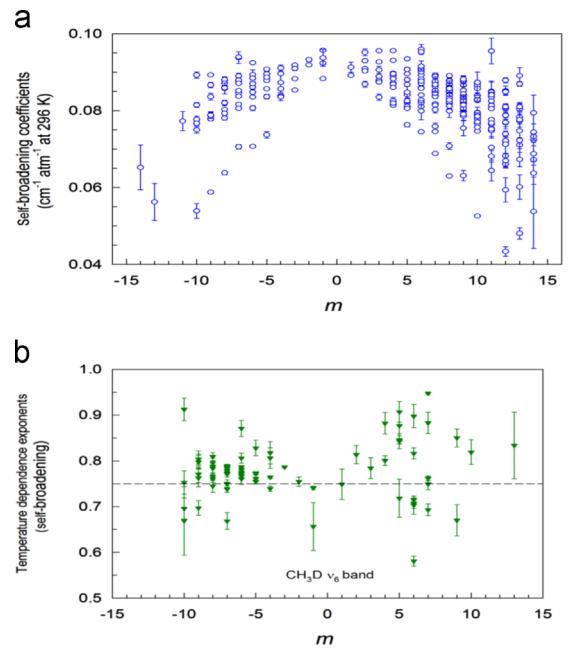


Fig. 5. Lorentz self-broadened line-width coefficients in units of $\text{cm}^{-1} \text{ atm}^{-1}$ in (a) and their temperature dependences (b) plotted against the quantum number index m for transitions in the ν_6 band of CH_3D . The dashed line in panel (b) represents the temperature dependence exponent value 0.75, often used as the default value for transitions where the exponent could not be experimentally determined.

recorded at 189 K and covering the Triad region between 1070 and 1540 cm^{-1} . Examples of multispectrum-fitted intervals are presented in Figs. 3 and 4. The top panel of Fig. 3 shows P-branch transitions with $J''=16$ and $K=0-12$ relevant to the ν_6 band. The top panel of Fig. 4 presents transitions from the $^R\text{Q}(J'', K''=0)$ series (band head near 1156.3 cm^{-1}) as well as transitions from the $^P\text{Q}(J'', K''=1)$ series (high-wavenumber side). In the bottom panels of both Figs. 3 and 4 we have plotted the weighted fit residuals (observed minus calculated) for all spectra included in the multispectrum fits.

The measured zero-pressure line position (ν) in cm^{-1} , N_2 -broadened line-width coefficient, $b_L^0(\text{N}_2)$ in $\text{cm}^{-1} \text{ atm}^{-1}$ at 296 K, N_2 -pressure-shift coefficient $\delta^\circ(\text{N}_2)$ in $\text{cm}^{-1} \text{ atm}^{-1}$ at 296 K, and their temperature dependences n_1 (unitless) and δ' ($\text{cm}^{-1} \text{ atm}^{-1} \text{ K}^{-1}$) are listed in Table 5. Despite the relatively low pressures of CH_3D in our gas samples, in many cases it was necessary to adjust the self-broadened line-width coefficients and their temperature dependence exponents to fit all spectra satisfactorily, and the resulting values determined from the fits are listed in Table 5 and plotted in Fig. 5.

As stated earlier, it was not possible to unambiguously determine from our spectra the CH_3D self-shift coefficients or temperature dependences, and they are not reported here.

In Fig. 5a we have plotted the room-temperature self-broadening coefficients in units of $\text{cm}^{-1} \text{ atm}^{-1}$ against the quantum index m for transitions in the ν_6 band of CH_3D . Here, $m=J''+1$ for the R-branch, $m=J''$ for the Q-branch, and $m=-J''$ for the P-branch transitions, where J is the rotational quantum number of the lower state. The points on Fig. 5 and

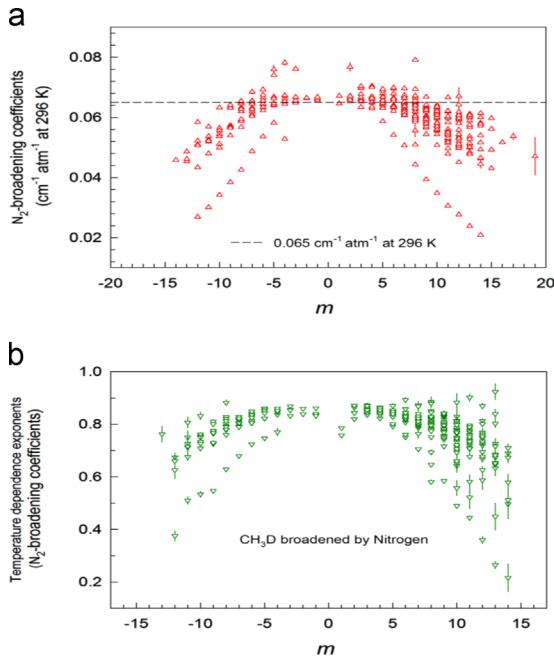


Fig. 6. Lorentz N₂-broadened line-width coefficients (a) and their temperature dependences (b) plotted against the rotational quantum index *m* for transitions in the ν_6 band of CH₃D. The dashed line represents the mean N₂-broadened line-width coefficient for transitions of this band. N₂-shift coefficients (a) and their temperature dependences (b) plotted against the rotational quantum index *m* for transitions in the ν_6 band of CH₃D. The dashed line in panel (a) represents the zero-shift value. The error bars represent one standard deviation. In this analysis the temperature dependence for N₂-pressure-shift coefficients were measured where appropriate. For unmeasured transitions their values were fixed to a default value of +0.00002 cm⁻¹ atm⁻¹ K⁻¹. This assumption introduced no noticeable residuals in the least squares fits.

6 with smaller broadening coefficients correspond to $P(J'',K'')$ and $R(J'',K'')$ transitions for which $J''=K''$. To aid in theoretical calculations we are providing the expression for these smaller broadening coefficients as a function:

$$b_L^0(\text{self}) = 7 \times 10^{-6} m^3 - 0.0004 m^2 - 0.0005 m + 0.0899. \quad (6)$$

The measured self-temperature dependence exponents are plotted in panel (b) of the same figure.

Similarly, in Fig. 6 we present our experimental results for N₂-broadening coefficients in panel (a) and their temperature-dependence exponents panel (b), both plotted against values of *m*. As we did for Fig. 5, the expression for the smaller $J''=K''$ broadening coefficients is:

$$\begin{aligned} b_L^0(N_2) = & -1 \times 10^{-8} m^5 + 1 \times 10^{-6} m^4 + 1 \times 10^{-6} m^3 \\ & - 0.0004 m^2 + 4 \times 10^{-5} m + 0.0678. \end{aligned} \quad (7)$$

Both the N₂- and self-broadening coefficients from the present study are in very good agreement with the room-temperature values determined in Ref. [35]. The N₂- and self- broadening temperature dependence exponents determined here for the ¹²CH₃D ν_6 band were found to be of similar magnitude as the temperature dependences experimentally determined for air- and self-broadened ¹²CH₄ and ¹³CH₄ transitions in the same spectral region

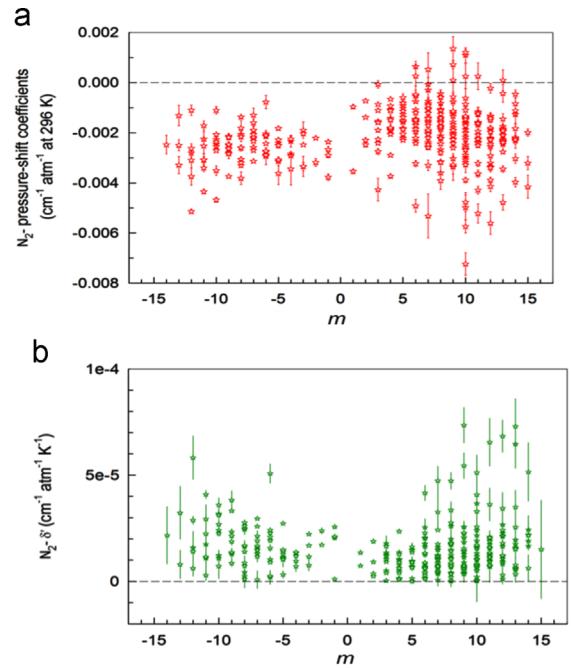


Fig. 7. N₂-shift coefficients (a) and their temperature dependences (b) plotted against the quantum index *m* for transitions in the ν_6 band of CH₃D. The dashed line in panel (a) represents the zero-pressure value. The error bars represent one standard deviation. In this analysis the temperature dependence for N₂-pressure-shift coefficients were measured where appropriate. For unmeasured transitions their values were fixed to a default value of +0.00002 cm⁻¹ atm⁻¹ K⁻¹. This assumption introduced no noticeable residuals in the least squares fits.

over a smaller temperature range [50–53]. We also note that for the four ν_6 transitions also measured by Varanasi and Chudamani [43] over the range from 123 K to 295 K, our N₂- and self-widths and temperature dependence exponents (measured over a larger temperature range) are in reasonable agreement within the absolute uncertainties of the two studies.

Our measured N₂-shift coefficients that are included in Table 5 and plotted in Fig. 7 lie between -0.007 and 0.002 cm⁻¹ atm⁻¹ at 296 K. The retrieved temperature-dependences for N₂- pressure-shift coefficients have also been plotted as a function of *m* in Fig. 7(b)). It is difficult to recognize a trend in the values for the retrieved N₂-shift coefficients due to the relatively small number of data points. However, we do note that the N₂-shift coefficients from the present study are very close to the room-temperature values determined in Ref. [35], and the N₂-shift temperature dependence coefficients determined here for the ¹²CH₃D ν_6 band are quite similar in magnitude to temperature dependences experimentally determined for air-broadened ¹²CH₄ shifts in the ν_4 band [50].

Fig. 8 presents overlaid experimental and calculated *J*-dependences of room-temperature CH₃D-N₂ broadening coefficients at various *K* values for two sub-branches R^R and P^R in the ν_6 band. The agreement between theoretical and retrieved N₂-broadening coefficients is best for *K* values below 7. Unfortunately the *J*-range of our retrieved line parameters is much smaller than that of theoretical

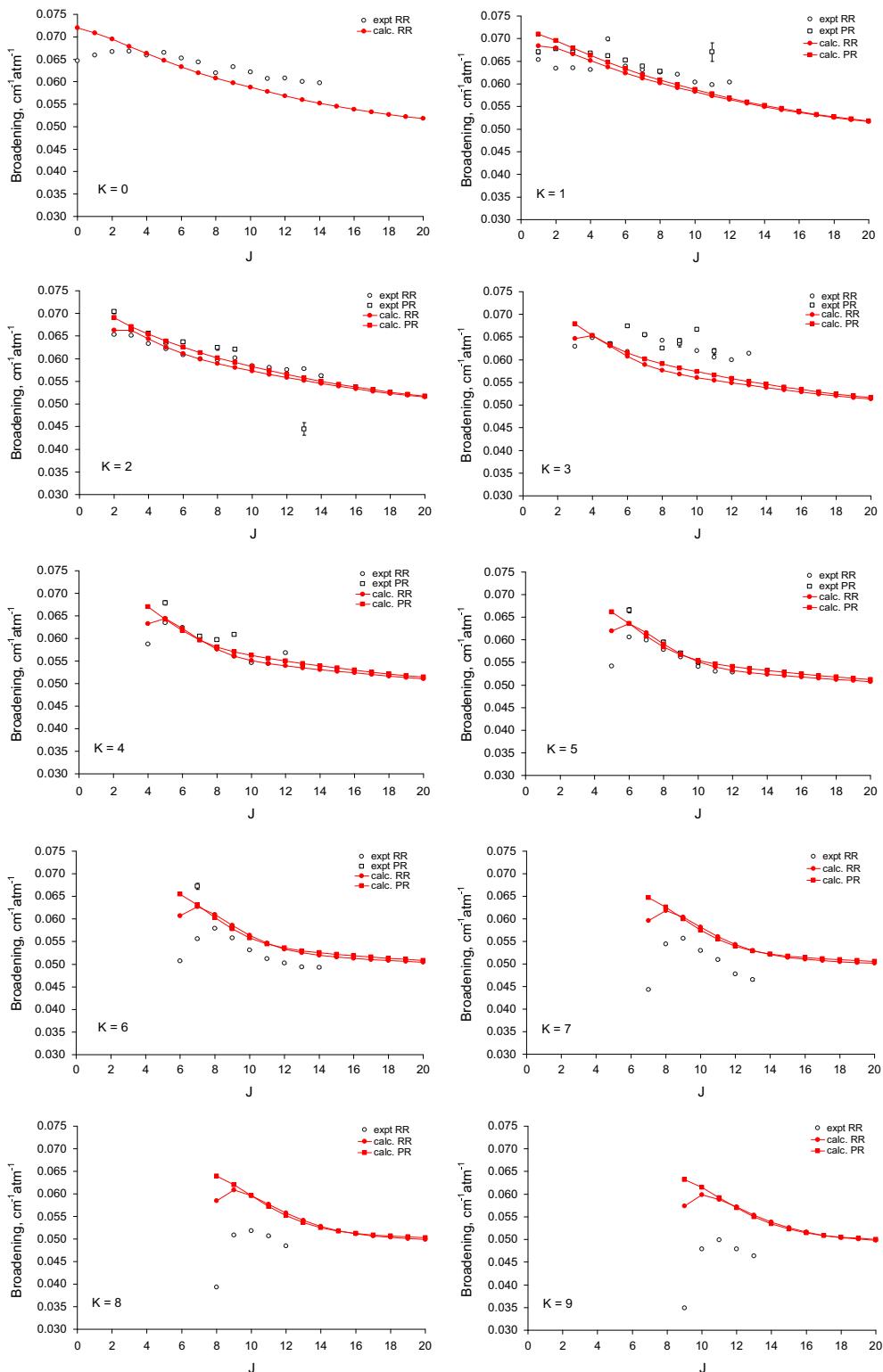


Fig. 8. Comparison of experimental and calculated J -dependences of room-temperature $\text{CH}_3\text{D}-\text{N}_2$ broadened line-width coefficients at various K values for the two sub-branches ${}^R\text{R}$ and ${}^P\text{R}$ in the ν_6 band.

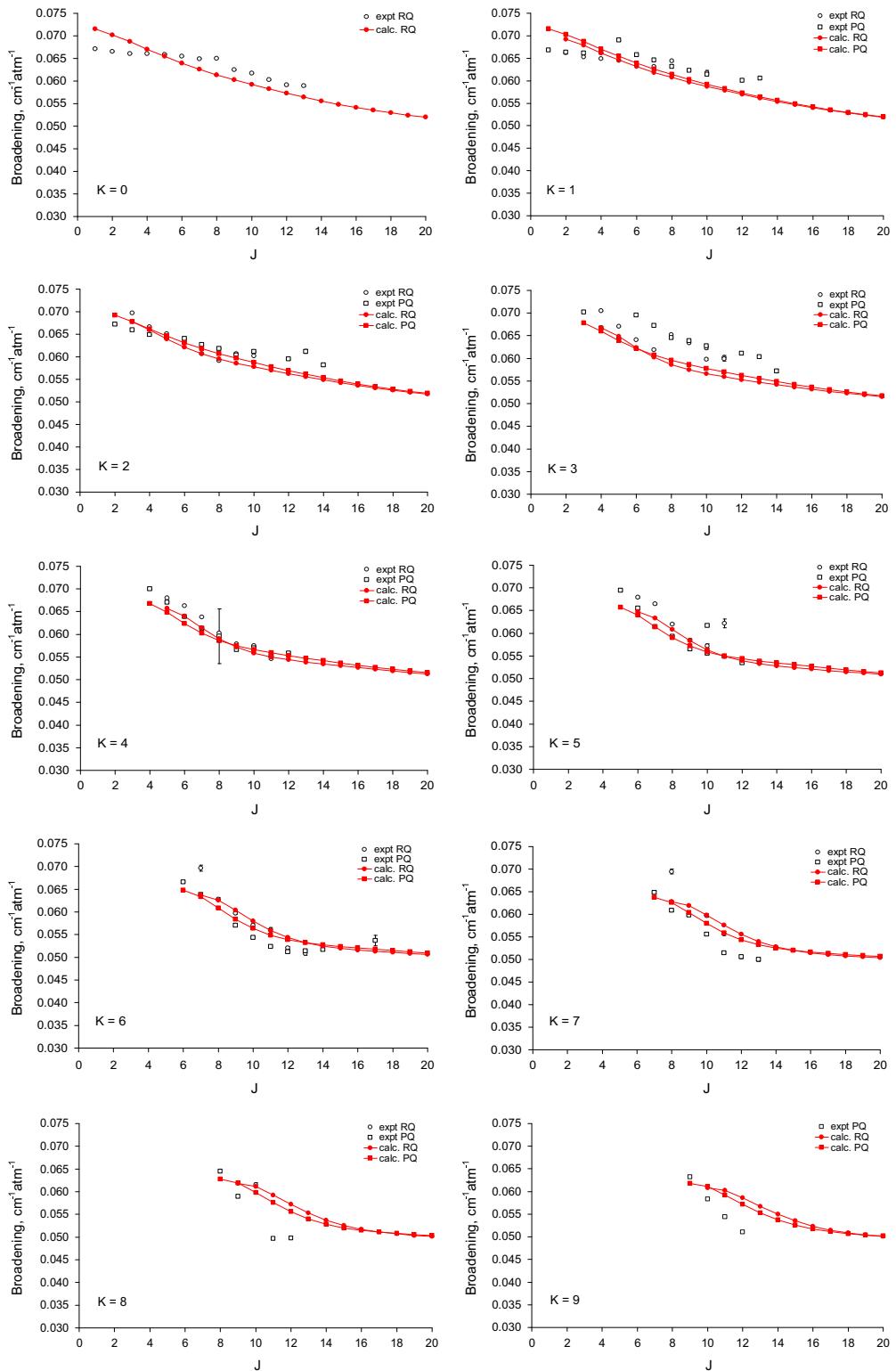


Fig. 9. Comparison of experimental and calculated J -dependences of room-temperature $\text{CH}_3\text{D}-\text{N}_2$ broadened line-width coefficients at various K values for the two sub-branches ${}^R\text{Q}$ and ${}^P\text{Q}$ in the ν_6 band.

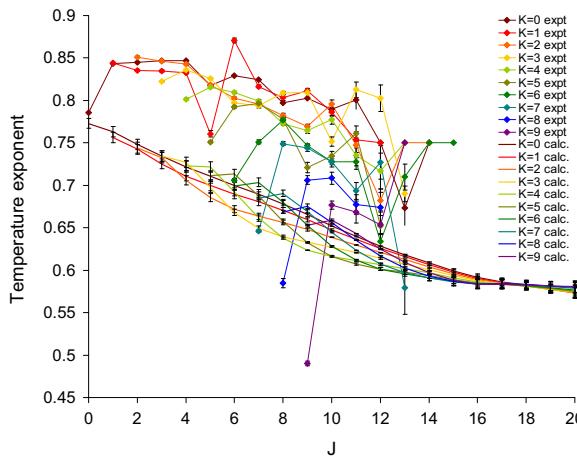


Fig. 10. Theoretical J -dependences of the temperature dependence exponents in comparison with the experimental values for ${}^R\text{R}$ -lines.

calculations and we are unable to check the agreement between the two sets of values at high J values.

In Fig. 9 we compare retrieved and calculated J -dependences of room-temperature $\text{CH}_3\text{D}-\text{N}_2$ broadening coefficients at various K values for the two sub-branches ${}^R\text{Q}$ and ${}^P\text{Q}$ in the ν_6 band. As in the case of the R-branch transitions, the calculations agree better with the experimental values for K below 7. Overall, the calculated N_2 -broadening coefficients show reasonable agreement with the retrieved N_2 -broadening coefficients but for K values above 6, they do not reproduce closely the trends in the retrieved line parameters. The general trend in the N_2 -broadening coefficients is to remain nearly constant for K values below 4, then to drop off rapidly to lower values for larger K values. The observed trends in the calculated and observed N_2 -broadening coefficients may arise from approximations made in the descriptions of wavefunctions of CH_3D . The calculations performed here are not at the level of accuracy of the tensorial formalism used in the global analysis of positions and intensities of CH_3D .

In order to deduce the temperature dependence exponents for $\text{CH}_3\text{D}-\text{N}_2$ lines we further calculated the broadening coefficients for two other experimentally probed temperatures: 240 K and 190 K. Lower temperatures were not considered since the thermal motion energy at those temperatures becomes close to the isotropic potential depth ($\varepsilon=83.50$ K) and the semi-classical approaches lose their validity. The temperature exponents N were extracted by the usual least-squares method from the relation:

$$\gamma_{if}(T) = \gamma_{if}(T_0) \times \left(\frac{T}{T_0}\right)^{-N} \quad (8)$$

where N is the n_1 of Eq. (1) and T_0 is 296 K, the reference temperature. (In Eq. (8) above, γ =line-broadening coefficient for $\text{CH}_3\text{D}-\text{N}_2$ and $N=n_1$ of Eq. (1).)

An example of their comparison with the experimental values is given in Fig. 10 for ${}^R\text{R}$ -branch lines. This figure shows that the theoretical values are generally lower than the corresponding measurements and that for the highest considered J , the differences between the calculated curves

for various K disappear. The discrepancies, as previously can be attributed to the drawbacks of the semi-classical treatment and the interaction potential model. Theoretical values for line-broadening coefficients at 296 K and the associated temperature exponents are included in Table 5.

A Voigt line shape including line mixing via full relaxation matrix formulation was used to fit the data and improve the residuals. The pressure and path-length products for our spectra listed in Table 1 were not large enough in order to distinguish easily speed-dependence and line-mixing effects. Hence, the speed-dependence parameters could not be retrieved in our analysis, and it was possible to measure the off-diagonal relaxation matrix elements (ORME) for N_2 -broadening only for the sets of transitions included in Table 6. We have been able to retrieve the temperature dependences for the relaxation matrix elements for only a few $\text{CH}_3\text{D}+\text{N}_2$ cases, using an exponential temperature dependence law similar to that used for broadening coefficients. The results for these parameters are also included in Table 6.

6. Conclusions

This study reports experimental measurements of N_2 -broadening and pressure-shift coefficients as a function of temperature in the ν_6 band of CH_3D . For the line-broadening case, semi-classical calculations are provided as well. A set of 23 spectra have been analysed to provide accurate values for zero-pressure line-center positions, self- and N_2 -broadening coefficients and self- and N_2 -pressure-shift coefficients for 400 transitions and their temperature dependences. We have identified several interesting patterns in the measured N_2 -broadening coefficients. In addition we have retrieved line mixing (off-diagonal relaxation matrix elements) and where possible, their temperature dependence exponents.

The agreement between the retrieved N_2 -broadening coefficients and the semi-classical theoretical results is good, except for higher K values where the theoretical results seem to be overestimated. Unfortunately, the experimental N_2 -pressure shift coefficients are generally

Table 6

Zero-pressure line positions, width and shift parameters and the off-diagonal relaxation matrix-element coefficients, W_{ij} , determined for pairs of sub-band transitions in the ν_6 band of $^{12}\text{CH}_3\text{D}$. The fixed parameters are reported with a "(F)" label attached to them.

Position ^a	$b_L^0(\text{N}_2)$ ^b	$n b_L^0(\text{N}_2)$	$\delta^0(\text{N}_2)$ ^b	$\delta'(\text{N}_2)$ ^d	Assignment	$W_{ij}(\text{N}_2)$ ^b	T-dep. $W_{ij}(\text{N}_2)$ ^b	$W_{ij}(\text{N}_2)$ ^e
1085.625324 (8)	0.0633 (2)	0.832 (15)	-0.00110 (15)	+0.000027(2)	$P^P(10,3,\text{A}1)$	0.0040 (2)	1.24 (19)	0.0031 (4)
1085.738824 (8)	0.0633 (2) ^c	0.832 (15) ^c	-0.00110 (15) ^c	+0.000027(2) ^c	$P^P(10,3,\text{A}2)$			
1094.044024 (5)	0.0642 (2)	0.774 (6)	-0.00214 (11)	+0.000023 (1)	$P^P(9,3,\text{A}2)$	0.0048(1)	0.75 (F)	0.0049 (2)
1094.117524 (5)	0.0642 (2) ^c	0.774 (6) ^c	-0.00214 (11) ^c	+0.000023 (1) ^c	$P^P(9,3,\text{A}1)$			
1102.423989 (4)	0.0655 (2)	0.779 (8)	-0.00215 97)	+0.000025 (1)	$P^P(8,3,\text{A}1)$	0.0045 (2)	0.82(9)	0.0045 (2)
1102.468792 (4)	0.0655 (2) ^c	0.779 (8) ^c	-0.00215 97) ^c	+0.000025 (1) ^c	$P^P(8,3,\text{A}2)$			
1110.754522 (7)	0.0645 (1)	0.805 (1)	-0.00218 (4)	+0.000026 (1)	$P^P(7,3,\text{A}2)$	0.0034 (1)	0.75 (F)	0.0060 (3)
1110.779654 (12)	0.0655 (2) ^c	0.779 (8) ^c	-0.00215 97) ^c	+0.000025 (1) ^c	$P^P(7,3,\text{A}1)$			
1119.025382 (8)	0.0675 (0)	0.814 91)	-0.00210 (3)	+0.000023 (0)	$P^P(6,3,\text{A}2)$	0.0048 (1)	0.75 (2)	0.0032 (2)
1119.038034 (12)	0.0675 (0) ^c	0.814 91) ^c	-0.00210 (3) ^c	+0.000023 (0) ^c				
1143.527534 (7)	0.0653 (1)	0.783 (3)	-0.00177 (5)	-0.000004 (0)	$R^Q(8,3,\text{A}2)$	0.0031 (1)	0.80 (F)	0.0032 (2)
1143.571634 (8)	0.0653 (1) ^c	0.783 (3) ^c	-0.00177 (5) ^c	-0.000004 (0) ^c	$R^Q(8,3,\text{A}1)$			
1154.439430 (16)	0.0590 (2)	0.840 (19)	-0.00186 (12)	-0.000018 (3)	$R^Q(13,0,\text{A}2)$			
1154.713917 (12)	0.0591 (1)	0.870 (12)	-0.00135 (11)	+0.000008 (2)	$R^Q(12,0,\text{A}1)$	0.00182 (29)	0.75 (F)	
1154.966470 (9)	0.0603 (1)	0.769 (7)	-0.00158 (9)	+0.000013 (2)	$R^Q(11,0,\text{A}2)$	0.00385 (27)	0.75 (F)	
1155.199670 (8)	0.0618 (1)	0.776 (4)	-0.00110 (7)	+0.000016 (1)	$R^Q(10,0,\text{A}1)$	0.00492 (22)	0.75 (F)	
1155.422423 (7)	0.0625 (1)	0.790 (3)	-0.00116 (7)	+0.000004 (1)	$R^Q(9,0,\text{A}2)$	0.00465 (11)	0.75 (F)	
1155.521843 (7)	0.0650 (1)	0.822 (3)	-0.00267 (7)	+0.000018 (1)	$R^Q(8,0,\text{A}1)$	0.00561 (15)	0.75 (F)	
1155.728731 (7)	0.0649 (1)	0.824 (2)	-0.00203 (5)	+0.000016 (1)	$R^Q(7,0,\text{A}2)$	0.00734 (10)	0.75 (F)	
1155.879355 (7)	0.0655 (1)	0.831 91)	-0.00146 (6)	+0.000013 (1)	$R^Q(6,0,\text{A}1)$	0.00628 (8)	0.75 (F)	
1156.004835 (13)	0.0659 91)	0.828 91)	-0.00186 (6)	+0.000007 (1)	$R^Q(5,0,\text{A}2)$	0.00625 (6)	0.75 (F)	
1156.108549 (7)	0.0660 (1)	0.855 (1)	-0.00206 (6)	+0.000005 (1)	$R^Q(4,0,\text{A}1)$	0.00674 (6)	0.75 (F)	
1156.191028 (7)	0.0660 (1)	0.840 (2)	-0.00190 (7)	-0.000000 (1)	$R^Q(3,0,\text{A}2)$	0.00435 (5)	0.75 (F)	
1156.252680 (8)	0.0666 (1)	0.820 (2)	-0.00248 (9)	-0.000009 (1)	$R^Q(2,0,\text{A}1)$	0.00279 (5)	0.75 (F)	
1156.293622 (11)	0.0671 (1)	0.758 (2)	-0.00354 (9)	+0.000014 (1)	$R^Q(1,0,\text{A}2)$			
1162.997143 (10)	0.0639 (1)	0.778 (2)	-0.00124 (4)	+0.000014 (1)	$R^Q(9,3,\text{A}1)$	0.0050 (1)	0.80 (F)	
1163.110746 (7)	0.0639 (1) ^c	0.778 (2) ^c	-0.00124 (4) ^c	+0.000014 (1) ^c	$R^Q(9,3,\text{A}2)$			
1163.714357 (8)	0.0645 (1)	0.826 (2)	-0.00212 (4)	+0.000026 (1)	$R^Q(8,3,\text{A}2)$	0.0048 (1)	1.17 (3)	
1163.787924 (8)	0.0645 (1) ^c	0.826 (2) ^c	-0.00212 (4) ^c	+0.000026 (1) ^c	$R^Q(8,3,\text{A}1)$			
1164.381569 (5)	0.0672 (1)	0.828 (2)	-0.00239 (3)	+0.000024 (0)	$R^Q(7,3,\text{A}1)$	0.0035 (1)	0.78 (5)	
1164.426483 (5)	0.0672 (1) ^c	0.828 (2) ^c	-0.00239 (3) ^c	+0.000024 (0) ^c	$R^Q(7,3,\text{A}2)$			
1164.989362 (4)	0.0696 91)	0.843 (2)	-0.00232 (3)	+0.000025 (0)	$R^Q(6,3,\text{A}2)$	0.0063 (1)	1.04 (3)	
1165.014728 (4)	0.0696 91) ^c	0.843 (2) ^c	-0.00232 (3) ^c	+0.000025 (0) ^c	$R^Q(6,3,\text{A}1)$			
1203.493135 (28)	0.0571 (2)	0.765 (5)	-0.00263 (5)	+0.000020 (1)	$R^P(12,3,\text{A}1)$	0.0031 (3)	0.75 (F)	
1203.505090 (26)	0.0571 (2) ^c	0.765 (5) ^c	-0.00263 (5) ^c	+0.000020 (1) ^c	$R^P(12,3,\text{A}2)$			
1205.485111 (8)	0.0655 (1)	0.794 (2)	-0.00140 (3)	+0.000002 (0)	$R^R(7,3,\text{A}2)$	0.0035 (1)	0.78 (5)	0.0001 (3)
1205.529251 (8)	0.0655 (1) ^c	0.794 (2) ^c	-0.00140 (3) ^c	+0.000002 (0) ^c	$R^R(7,3,\text{A}1)$			
1212.252462 (6)	0.0642 (1)	0.809 (2)	-0.00123 (3)	+0.000003 (0)	$R^R(8,3,\text{A}2)$	0.0064 91)	1.14 (2)	0.0038 (4)
1212.298834 (8)	0.0642 (1) ^c	0.809 (2) ^c	-0.00123 (3) ^c	+0.000003 (0) ^c	$R^R(8,3,\text{A}1)$			
1218.616479 (8)	0.0674 (2)	0.872 (5)	-0.00206 (7)	+0.000012 (1)	$R^R(6,3,\text{A}1)$	0.0043 (2)	1.23 (8)	
1218.661262 (9)	0.0674 (2) ^c	0.872 (5) ^c	-0.00206 (7) ^c	+0.000012 (1) ^c	$R^R(6,3,\text{A}2)$			
1218.933810 (9)	0.0641 (0) ^c	0.809 (0) ^c	-0.00201 (4) ^c	+0.000002 (0) ^c	$R^R(9,3,\text{A}1)$	0.0111(1)	1.09 (0)	
1218.969303 (6)	0.0641 (0)	0.809 (0)	-0.00201 (4)	+0.000002 (0)	$R^R(9,3,\text{A}2)$			
1225.452547 (7)	0.0620 (1)	0.752 (6)	-0.00227 (4)	+0.000016 (1)	$R^R(10,3,\text{A}2)$	0.0064 (1)	0.94 (7)	0.0018 (5)
1225.488360 (7)	0.0674 (2) ^c	0.872 (5) ^c	-0.00206 (7) ^c	+0.000012 (1) ^c	$R^R(10,3,\text{A}1)$			
1225.671923 (9)	0.0656 (1)	0.829 95)	-0.00318 (7)	+0.000018 (1)	$R^R(7,3,\text{A}2)$	0.0044 (2)	1.05 (8)	
1225.745502 (9)	0.0656 (1) ^c	0.829 95) ^c	-0.00318 (7) ^c	+0.000018 (1) ^c	$R^R(7,3,\text{A}1)$			
1231.811182 (9)	0.0606 (1)	0.813 (9)	-0.00142 (5)	+0.000021 (1)	$R^R(11,3,\text{A}1)$	0.0061 (1)	1.12(11)	0.0038 (1)
1231.848733 (9)	0.0606 (1) ^c	0.813 (9) ^c	-0.00142 (5) ^c	+0.000021 (1) ^c	$R^R(11,3,\text{A}2)$			
1238.006728 912)	0.0599 (2)	0.803 (16)	-0.00191 (6)	+0.000015 (1)	$R^R(12,3,\text{A}2)$	0.0063 (2)	0.90 (19)	
1238.044758 (12)	0.0599 (2) ^c	0.803 (16) ^c	-0.00191 (6) ^c	+0.000015 (1) ^c	$R^R(12,3,\text{A}1)$			
1244.037172 (17)	0.0614 (2)	0.690(10)	-0.00220 (8)	-0.000017 (2)	$R^R(13,3,\text{A}1)$	0.0060 (3)	0.75 (F)	
1244.072667 (17)	0.0614 (2) ^c	0.690(10) ^c	-0.00220 (8) ^c	-0.000017 (2) ^c	$R^R(13,3,\text{A}2)$			

^a cm^{-1} .^b $\text{cm}^{-1} \text{ atm}^{-1}$ at 296 K.^c These values are constrained to be the same for the two split pairs of transitions.^d $\text{cm}^{-1} \text{ atm}^{-1} \text{ K}^{-1}$.^e Reference [35]: only room temperature off-diagonal relaxation matrix element coefficients were determined.

scattered and we were unable to model them with our theoretical model.

Acknowledgments

The research described in this article was carried out at the College of William and Mary, Jet Propulsion Laboratory (JPL), California Institute of Technology, Connecticut College and NASA Langley Research Center under contracts with the National Aeronautics and Space Administration. A. Predoi-Cross acknowledges the support she received from the National Sciences and Engineering Research Council of Canada and the study leave program at the University of Lethbridge, AB, Canada for providing the opportunity to carry out this investigation. The authors thank NASA's UPPER Atmosphere Research Program for their support of the McMath – Pierce FTS laboratory.

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