

Answers to Exercise 3.1

Calculating Frequency, Wavelength and Energy of Light

Always check your work when you finish a calculation!

Is the answer reasonable? Check sig. fig.

1. $c = v\lambda$

$$v = \frac{c}{\lambda} = \frac{2.997925 \times 10^8 \frac{m}{s}}{365 \text{ nm}} \times \frac{10^9 \text{ nm}}{1 \text{ m}} \times \frac{1 \text{ Hz}}{1 \frac{1}{s}} = 8.21 \times 10^{14} \text{ Hz}$$

2. $E_{\text{photon}} = hv$

$$E_{\text{photon}} = \left(6.626070 \times 10^{-34} \frac{\text{J}}{\text{Hz}} \right) (2.4 \times 10^{16} \text{ Hz}) = 1.6 \times 10^{-17} \text{ J}$$

3. $E_{\text{photon}} = hv$ and $c = v\lambda$

$$E_{\text{photon}} = \frac{hc}{\lambda} = \frac{(6.626070 \times 10^{-34} \frac{\text{J}}{\text{Hz}}) (2.997925 \times 10^8 \frac{m}{s})}{12 \mu\text{m}} \times \frac{1 \text{ Hz}}{1 \frac{1}{s}} \times \frac{10^6 \mu\text{m}}{1 \text{ m}} = 1.7 \times 10^{-20} \text{ J}$$

4. **Step 1: Convert energy of photon into SI units**

$$E = 17.1400 \text{ eV} \times \frac{1.60217565 \times 10^{-19} \text{ J}}{1 \text{ eV}} = 2.74613 \times 10^{-18} \text{ J}$$

Step 2: Calculate frequency from energy

$$E = hv$$

$$v = \frac{E}{h} = \frac{2.74613 \times 10^{-18} \text{ J}}{6.626070 \times 10^{-34} \frac{\text{J}}{\text{Hz}}} = 4.14443 \times 10^{15} \text{ Hz}$$

Step 3: Calculate wavelength from frequency

$$c = v\lambda$$

$$\lambda = \frac{c}{v} = \frac{2.997925 \times 10^8 \frac{m}{s}}{4.14443 \times 10^{15} \text{ Hz}} \times \frac{1 \text{ Hz}}{1 \frac{1}{s}} = 7.23362 \times 10^{-8} \text{ m}$$

$$\lambda = \frac{c}{v} = 7.23362 \times 10^{-8} \text{ m} \times \frac{10^9 \text{ nm}}{1 \text{ m}} = 72.3362 \text{ nm}$$

5. **Step 1: Calculate the energy of one photon of blue light ($\lambda = 475 \text{ nm}$)**

$$E_{\text{photon}} = hv \quad \text{and} \quad c = v\lambda$$

$$E_{\text{photon}} = \frac{hc}{\lambda} = \frac{(6.626070 \times 10^{-34} \frac{\text{J}}{\text{Hz}}) (2.997925 \times 10^8 \frac{m}{s})}{475 \text{ nm}} \times \frac{1 \text{ Hz}}{1 \frac{1}{s}} \times \frac{10^9 \text{ nm}}{1 \text{ m}} = 4.18 \times 10^{-19} \text{ J}$$

Step 2: Calculate the number of photons in the light beam

$$E_{\text{total}} = E_{\text{photon}} \times \# \text{photons}$$

$$\# \text{photons} = \frac{E_{\text{total}}}{E_{\text{photon}}} = \frac{2.50 \times 10^{-16} \text{ J}}{4.18 \times 10^{-19} \frac{\text{J}}{\text{photon}}} = 598 \text{ photons}$$