## Answers to Exercise 9.5

Nonstandard Potential for Electrochemical Cells: The Nernst Equation!

1. Step 1: Find $v_{e}$ and $\boldsymbol{E}^{\circ}$ by balancing redox equation

Oxidation:

$$
M n_{(s)} \rightarrow M n_{(a q)}^{2+}+2 e^{-} \quad E^{\circ}=+1.185 V
$$

Reduction:

$$
\begin{aligned}
& - \\
& =2
\end{aligned}
$$

Therefore, $v_{e}=2$
Step 2: Determine activities for all reactants and products
$a_{M n_{(s)}}=1$

$$
a_{P b_{(a q)}^{2+}}=\frac{0.0125 M}{1 M}=0.0125
$$

$$
\begin{aligned}
& a_{M n_{(a q)}^{2+}}=\frac{0.0375 M}{1 M}=0.0375 \\
& a_{P b_{(s)}}=1
\end{aligned}
$$

Step 3: Calculate reaction quotient
$Q=\frac{\left(a_{M n_{(a q)}^{2+}}\right)\left(a_{P b_{(s)}}\right)}{\left(a_{M n_{(s)}}\right)\left(a_{P b_{(a q)}^{2+}}\right)}=\frac{(0.0375)(1)}{(1)(0.0125)}=3.00$
Step 4: Calculate potential for reaction under nonstandard conditions
$E=E^{\circ}-\frac{R T}{v_{e} F} \ln Q$
$E=(1.060 \mathrm{~V})-\frac{\left(8.314462 \frac{\mathrm{~J}}{\text { mol- } \mathrm{K}}\right)(298.15 \mathrm{~K})}{(2)\left(96485 \frac{\mathrm{C}}{\mathrm{mol}}\right)} \ln (3.00) \times \frac{1 \mathrm{~V}}{1 \frac{\mathrm{~J}}{\mathrm{C}}}$
$E=1.060 \mathrm{~V}-0.014 \mathrm{~V}$
$E=1.046 \mathrm{~V}$
Step 5: Check your work
Does your answer seem reasonable?
2. $\quad$ This question requires you to work backward through the same process as in question 1. So, start with cell potential. Use it and reaction quotient to calculate standard potential. Then use standard potential to calculate the standard reduction potential of $\mathrm{Cu}_{(a q)}^{2+}$.
Step 1: Find $v e$ by balancing redox equation
Oxidation:

$$
C u_{(s)} \rightarrow C u_{(a q)}^{2+}+2 e^{-} \quad E^{\circ}=? ? ?
$$

Reduction (multiply by 2): $A g_{(a q)}^{+}+e^{-} \rightarrow A g_{(s)} \quad E^{\circ}=+0.7996 \mathrm{~V}$
Overall:

$$
C u_{(s)}+2 A g_{(a q)}^{+} \rightarrow C u_{(a q)}^{2+}+2 A g_{(s)} \quad E^{\circ}=? ? ?
$$

Therefore, $v_{e}=2$
Step 2: Determine activities for all reactants and products
$a_{C u_{(s)}}=1$
$a_{C u_{(a q)}^{2+}}=\frac{0.067 M}{1 M}=0.067$
$a_{A g_{(a q)}^{+}}=\frac{0.0084 M}{1 M}=0.0084$

$$
a_{A g_{(s)}}=1
$$

Step 3: Calculate reaction quotient
$Q=\frac{\left(a_{C u_{(a q)}^{2+}}\right)\left(a_{A g_{(s)}}\right)^{2}}{\left(a_{C u_{(s)}}\right)\left(a_{A g_{(a q)}^{+}}\right)^{2}}=\frac{(0.067)(1)^{2}}{(1)(0.0084)^{2}}=9.5 \times 10^{2}$

## Step 4: Calculate standard potential for reaction

$E=E^{\circ}-\frac{R T}{v_{e} F} \ln Q$
$E^{\circ}=E+\frac{R T}{v_{e} F} \ln Q$
$E^{\circ}=(0.3696 \mathrm{~V})+\frac{\left(8.314462 \frac{\mathrm{~J}}{\mathrm{~mol} \cdot \mathrm{~K}}\right)(298.15 \mathrm{~K})}{(2)\left(96485 \frac{\mathrm{C}}{\mathrm{mol}}\right)} \ln \left(9.5 \times 10^{2}\right) \times \frac{1 \mathrm{~V}}{1 \frac{J}{\mathrm{C}}}$
$E^{\circ}=0.3696 V+0.088 V$
$E^{\circ}=0.4577 \mathrm{~V}$
Step 5: Calculate standard half-cell potential for oxidation of $\mathbf{C u}$ to $\mathbf{C u}^{\mathbf{2 +}}$
$E^{\circ}{ }_{\text {cell }}=E^{\circ}{ }_{\text {oxidation half-cell }}+E^{\circ}{ }_{\text {reduction half-cell }}$
$E^{\circ}{ }_{\text {oxidation half-cell }}=E^{\circ}{ }_{\text {cell }}-E^{\circ}{ }_{\text {reduction half-cell }}$
$E^{\circ}{ }_{\text {oxidation half-cell }}=(0.4577 \mathrm{~V})-(0.7996 \mathrm{~V})$
$E^{\circ}{ }_{\text {oxidation half-cell }}=-0.3419 \mathrm{~V}$
Step 6: Calculate standard reduction potential for $\mathbf{C u}^{\mathbf{2 +}}$ to $\mathbf{C u}$
This is the reverse of the observed half-reaction, so multiply by -1
$E^{\circ}{ }_{C u^{2+} / C u}=-(-0.3419 \mathrm{~V})=+0.3419$

## Step 7: Check your work

Does your answer seem reasonable?
Most standard reduction potentials fall between +3 V and -3 V ; the calculated value falls within that range. Reference tables give values of approximately +0.34 V for the standard reduction potential of $\mathrm{Cu}^{2+}$.
3.
(a) Since there is no net reaction, the standard potential for this cell must be zero.

This is what is called a "concentration cell". The driving force for the reaction is the fact that the concentrations in the two half-cells are different.
(b) Positive.

A positive cell potential indicates a reaction that is product-favoured.
A concentration cell reaches equilibrium when the concentrations in the two half-cells become the same. In the cell as written, the concentration of $\mathrm{Zn}^{2+}$ in the reduction halfcell (the righthand side in cell notation) is higher than the concentration of $\mathrm{Zn}^{2+}$ in the oxidation half-cell (the lefthand side in cell notation). Thus, reduction of some $Z n^{2+}$ to $Z n$ in the reduction half-cell and oxidation of some Zn to $\mathrm{Zn}^{2+}$ in the oxidation half-cell will bring the two solution concentrations closer together.
Essentially, the following reaction is product-favoured:

$$
Z n_{(s)}+Z n_{(a q)}^{2+}(0.042 M) \rightarrow Z n_{(a q)}^{2+}(0.024 M)+Z n_{(s)}
$$

(c) Step 1: Find $v_{e}$ and $\boldsymbol{E}^{\circ}$ by balancing redox equation

| Oxidation: | $Z n_{(s)} \rightarrow Z n_{(a q)}^{2+}+2 e^{-}$ | $E^{\circ}=+0.7618 \mathrm{~V}$ |
| :--- | :--- | :--- |
| Reduction: | $Z n_{(a q)}^{2+}+2 e^{-} \rightarrow Z n_{(s)}$ | $E^{\circ}=-0.7618 \mathrm{~V}$ |
| Overall: | no net reaction | $E^{\circ}=0 \mathrm{~V}$ |
| Therefore, $v_{e}=2$ |  |  |

## Step 2: Determine activities for all reactants and products

$a_{Z n_{(s)}}=1$
$a_{Z n_{(a q)}^{2+}}=\frac{0.024 M}{1 M}=0.024$
$a_{Z n_{(a q)}^{2+}}=\frac{0.042 M}{1 M}=0.042$
$a_{Z n_{(s)}}=1$

Step 3: Calculate reaction quotient
$Q=\frac{\left(a_{Z n_{(a q)}^{2+}}\right)\left(a_{Z n_{(s)}}\right)}{\left(a_{\left.Z n_{(s)}\right)}\right)\left(a_{Z n_{(a q)}^{2+}}\right)}=\frac{(0.024)(1)}{(1)(0.042)}=0.57$

## Step 4: Calculate potential for reaction under nonstandard conditions

$E=E^{\circ}-\frac{R T}{v_{e} F} \ln Q$
$E=(0 \mathrm{~V})-\frac{\left(8.314462 \frac{\mathrm{~J}}{\text { mol. } \mathrm{K}}\right)(298.15 \mathrm{~K})}{(2)\left(96485 \frac{\mathrm{C}}{\text { mol }}\right)} \ln (0.57) \times \frac{1 \mathrm{~V}}{1 \frac{J}{\mathrm{C}}}$
$E=0 V-(-0.0072 V)$
$E=+0.0072 \mathrm{~V}$

## Step 5: Check your work

Does your answer seem reasonable?
It is consistent with the prediction from part (b) and has a reasonable order of magnitude.

